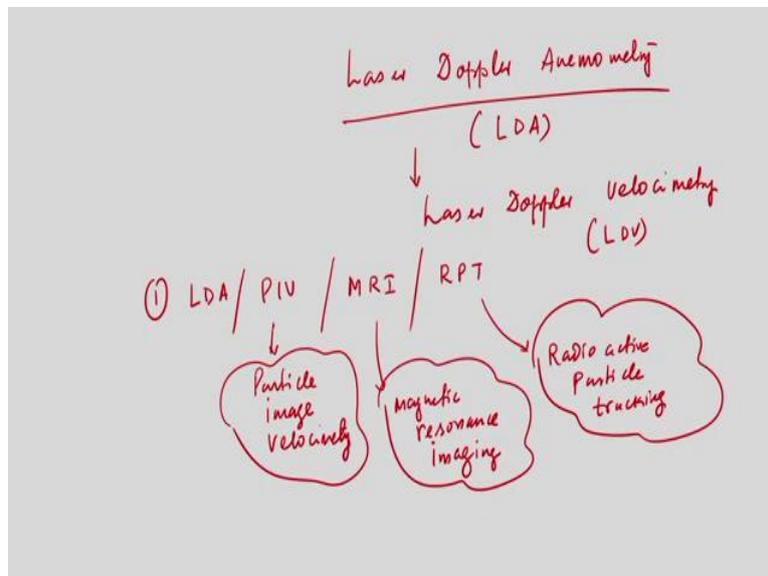


Experimental Methods in Fluid Mechanics
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Lecture 21

Laser Doppler Anemometry

Good afternoon, I welcome you to the session of Experimental Methods in Fluid Mechanics. And today, we will discuss about another Flow Measurement technique that is the instrument, rather the operational principle of the Laser Doppler Anemometry. In fact, this Laser Doppler Anemometry is an important noninvasive flow measurement technique and it is largely used to measure the flow velocity at a point.

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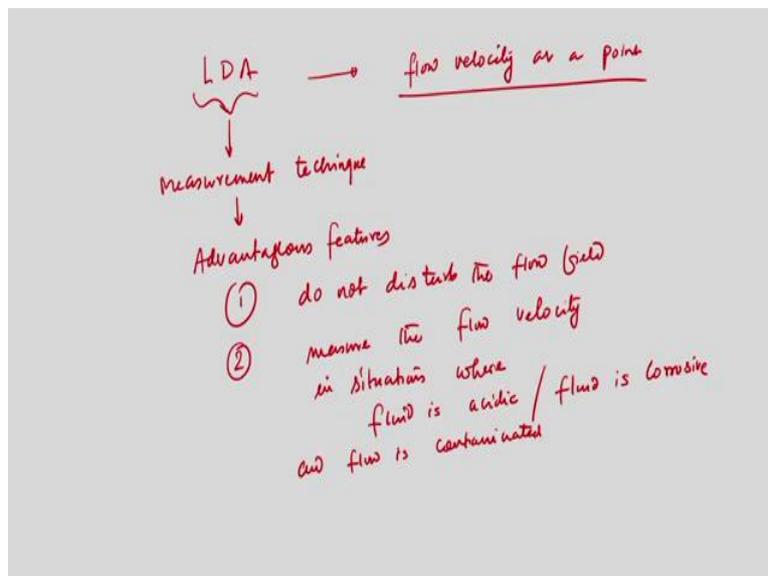
So, we will discuss today, this laser doppler anemometry. As I said that, laser doppler anemometry is an important noninvasive flow measurement technique which is used to measure, point flow, velocity at a point. Now, there are a few noninvasive techniques like so, this is LDA in short or sometimes it is also known as, Laser Doppler Velocimetry or LDV in short. Now, there are different other techniques which are noninvasive in nature and also used to measure the flow velocity, like I can say, LDA is one of them.

So, LDA, then we can have PIV, that we know that is Particle Image Velocimetry, then we have MRI, Magnetic Resonance Imaging, then we can have RPT. So, there are several other noninvasive measurement techniques available, which are used to measure velocity at a point. So, this is particle image velocimetry, this is magnetic resonance imaging, and this is radioactive particle tracking. So, these are the techniques which are used to measure flow

velocity and which are noninvasive in nature. Now, question is why you are going to discuss about laser doppler anemometry.

Laser doppler anemometry relies on the measurement of velocity on the, you know, that are image based, in which we need to have a source of light. Now, the word itself is, or the word itself is sufficient to know that, in our laser doppler anemometry, the light source is laser. Now, as I said that laser doppler anemometry is a noninvasive technique, there are a few advantages featured.

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So, when you talk about LDA, this instrument, this measurement techniques. So, this measurement technique which is having a few advantages feature, so which is having a few advantages features. Now, number 1, do not disturb the flow field. We have discussed that, we can have measurement of flow parameters using probe, we can have measurement of volumetric flow rate using flow obstruction flow meter. In fact, we have seen in the last class that, we can measure velocity using hot wire or hot film.

In all these cases, we need to insert the instrument, we need to insert the object in the flow field. Now, when we insert the object in the flow field definitely that, you know placing or, you know in position of that particular instrument in the flow field will try to disturb. And as a result, we may not get the accurate actual velocity which you are going to, you know measure from using that instrument. So, from their perspective, this technique that is Laser Doppler anemometry is having advantage.

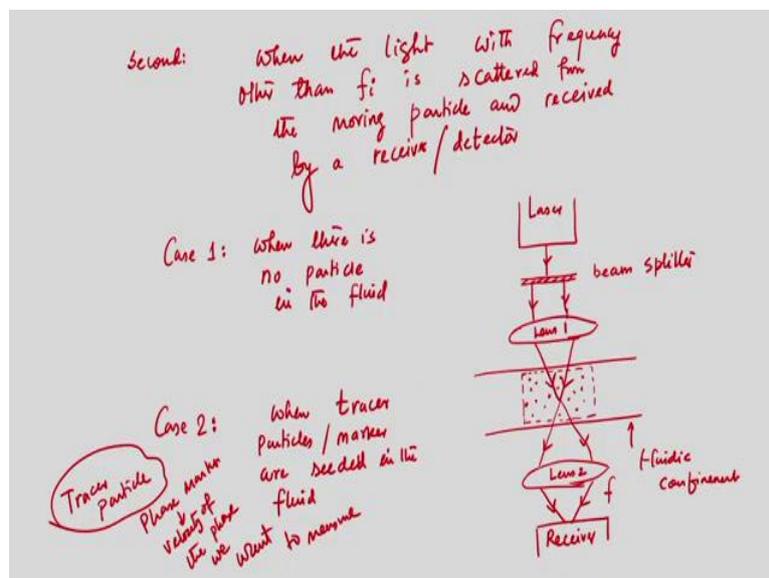
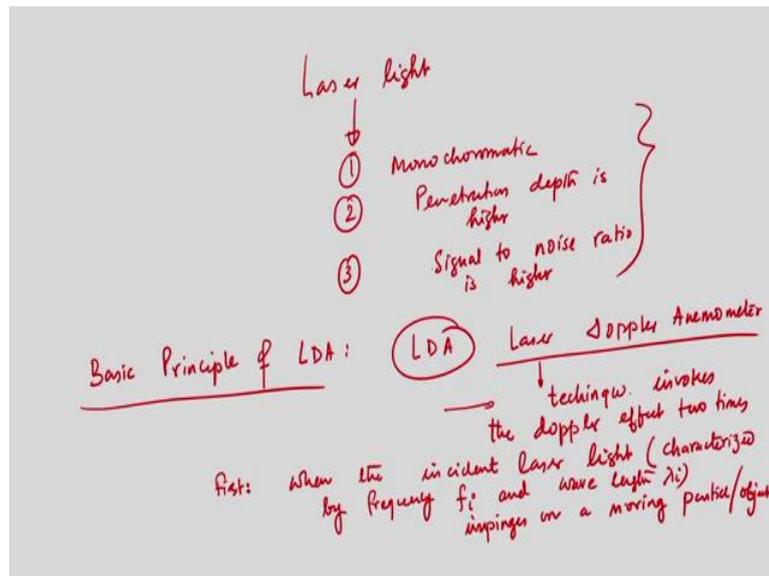
So, that is because, these technique do not disturb the flow field, and that is why the word noninvasive is came. Another important is that, this technique can be used to measure velocity in situations. So, it can be measured, this technique can be used to measure the flow velocity. So, when you talk about flow velocity, as I said this is used to have point flow measurement. So, this is used to measure velocity at a point. Now, measure the flow velocity, in situation where fluid is acidic, if the fluid is corrosive and flow is contaminated, with different foreign particles.

So, even again, if you would like to compare this technique with the other available techniques that we have discussed that hot film, hot wire, mechanical probe. In all these cases, we cannot, even if we use, I mean it will, the corrosive nature of the fluid, acidic nature of the fluid will try to, you know rather it will try to damage the measurement part, measurement points. If it is mechanical probe that will try to clog the point, clog the hole. If it is, you know hot wire, it will try to, you know tear the wire.

So, the presence of foreign particle and the different fluid properties like acidic, corrosive, these are not you know, I mean these properties are not important, rather we do not consider whether the fluid is acidic or corrosive or fluid is contaminated, while you are using LDA to measure the flow velocity.

So, these are the few advantages features which are associated with the LDA technique. Now, as I said that LDA that is laser Doppler anemometry and light source is the laser. Now, why we are using laser light, there are many other sources of light, instead we can use any radioactive also, radioactive wave, but we are using laser.

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Because laser light is also having, laser light is also having a few important points, rather important favorable points that we should discuss now, that laser light is monochromatic, penetration depth is higher, number 3, signal to noise ratio is also higher. So, accounting all this 3, rather these important points we are using laser as a light source. Now, we need to know what is the basic principle of measuring flow velocity using the LDA technique or laser doppler anemometry. So, the basic principle that we need to know of LDA. So, now we will discuss the basic principle.

So, up to this time, we have understood laser doppler anemometry is used to measure point velocity, this measurement is noninvasive, this measurement is not disturbed, rather do not disturb the flow field.

And using this technique we can have flow measurement, rather velocity measurement of flow velocity when fluid is toxic, fluid is acidic, fluid is corrosive and if the flow is contaminated, so we need not to consider at all. If you try to measure flow velocity using another instrument like, mechanical flow or hot field, then these, you know kind of contaminated flow, corrosiveness of the fluid will try to destroy the lifetime of those instruments. But this is not an important points that we should consider, when we are measuring flow velocity using laser doppler anemometry.

Now, as I said that this technique uses laser as a light source and then light is incidented on a object and from there we, receive one frequency. So, when our light is incidented on object, so, we have a frequency and when the light is incidental of the object, that light will be scattered now, and from that object we also try to capture, received the frequency. Now, the basic principle is LDA is that, I am writing now that this LDA that is Laser Doppler Anemometer. The word doppler is there, so we will be using doppler effects. We have studied doppler effects in our class, 2 level, at 10 plus 2 level physics.

So, we have seen what is doppler effect and again today, we will discuss why this doppler effect is coming into picture, when we talk about flow velocity measurement using LDA. So LDA, a technique is that, that doppler effect this technique, this techniques, you know, invokes the doppler effect 2 times. First, first when the light, rather incident laser light, which is characterized by frequency f_i and wavelength λ_i , when the incident laser light impinges on a moving particle or object.

So, the laser doppler anemometer technique, I can say this technique, this technique, doppler anemometry technique invokes the doppler effect 2 times. First, when the laser light, incident laser light which is characterized by the frequency f_i , wavelength λ_i impinges on a moving particle.

And second, second is when the light with frequency other than f_i is scattered from the moving particle and received by a receivers or detector. So, this is the basic principle, we incident laser light on a moving particle then, and we know the frequency and wavelength of the moving particle. And then second is, when the light is being scattered by the particle by the moving particle, the scattered light and the frequencies different then the f_i and that frequency is received by a receiver or a detector. So, now, this is the basic principle.

So, now, we will take an example, we will see how we can really measure, rather we can use this technique to measure the flow velocity. And till now, we have discuss about the laser light frequency and we will see that we need we can corelate the measured frequency with the fluid velocity. So, I can show you that say, we have a laser source. So, this is a laser source and the laser light is taken into a splitter, say this is beam splitter and the light is divided to 2 parts and taken into a lens.

And then from lens, we can focus the light in a zone of our interest, say if it is of our, if it is the zone of our interest and we are focusing the laser light and the light which is, you know scattered is again taken into a lens and that is, you know collected by receiver, so this is receiver. So, this is lens 2, this is lens 1 and this is receiver. So, say we would like to measure the flow velocity and this is the confinement. So, this is fluidic confinement and we would like to measure the velocity of the fluid that is flowing through this confinement using this laser doppler anemometer technique.

So, what is done, there is a laser source, light is coming, light is taken to a beam splitter, essentially to split the light incoming light into 2 parts. The splitted now, lights are taken into a lens essentially to focus that light on a zone which is the zone of our interest. And then from there, we again, we the, you know scattered light is taken by into a lens and finally, the frequency or length or light or wave that is you know received by the receiver.

Now, see I can tell you, now when there is no any particle then the light is coming say, I can tell that there is no any particle. So, light is coming and the light will be received by the receiver. So, there will get one kind of frequency at the receiver, frequency of the receiving it. Now, say another condition where I am giving a few tracer particle here, this tracer particles and this tracer particles are seeded in the fluid and particles are neutrally wind, so the tracer particle. So, case 1, I can write now, case 1, when there is no particles in the fluid. And case 2, when tracer particles, sometimes they are known as marker, are seeded in the fluid.

So, marker means they are used to you know, mark the phases. So, phase marker, velocity of the phase we want to measure. So, basically the tracer particle, tracer particle also known as phase marker, you know, that is, you know, velocity of the phase we want to measure. So, now tracer particles, when here, when the tracer particles are seeded in the fluid.

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✓ Tracer Particle \rightarrow very small
density $\rightarrow \rho_s =$ fluid density ρ_f

$(f + f_s)$
frequency received by the receiver when tracer particles are seeded

f
frequency of the signal received by the receiver when no particle is there is fluid

$f \neq f + f_s$ additional shift/shift in frequency

Second: when the light with frequency other than f_i is scattered from the moving particle and received by a receiver/detector

Case 1: when there is no particle in the fluid

Case 2: when tracer particles/marker are seeded in the fluid
Tracer particle
Plane marker
velocity of the plane we want to measure

Receiver $f + f_s + 2$

$f_s \rightarrow$ shift (frequency)
 \downarrow directly correlated to the fluid velocity

\rightarrow scattering of light by the particles
 \downarrow shift in frequency

Doppler effect

Now, the important characteristics of the tracer particle will be the density of the particle. So, the tracer particle, I am writing the tracer particle density is ρ_s and this is equal to the fluid density, ρ_f and tracer particles are very small. So, tracer particles which are seeded they are very small and density of the particle is equal to the density of the fluid, so that they can follow the flow. Now, that is they are neutrally buoyant. So, the particles which are seeded they will largely follow the flow direction and density is equal.

So, these 2 are the important, I know, I can say points we need to consider when we are you know seeding a tracer particle to essentially to measure the flow velocity. Now, if I go back to a previous slide, I can tell when there is no particle of course, the receiver will receive signal, the light which is falling on the object from the laser source and receiver will definitely receive a signal. In that case, if the signal frequency is f and the second case when we seeded up few particles and the particles when they are seeded, now when the light is, you know incidenting on the particle, they will try to transmit, transmit in different direction.

Now, there will be transmission directions which are in the direction of the receiver. So, when the particles are seeded in the fluid and particles are neutrally buoyant, they will follow the fluid motion, when the light is now falling, light falling on the particles, there will be a, you know scattering of the light by the particle in different direction, there will be direction of the scattered light, which is in the direction of the receiver. Say, in that case the signal received by the, this is for the 1, case 1 and in that case, $f + f_s$ and say this is for the case of 2 that is when a fluid is having a few seeded particle.

Now, obviously, this $f + f_s$, so $f + f_s$, so this is the frequency received by the receiver when tracer particles are seeded, while f is the frequency of the signal or light received by the receiver when no particles, no particle is there in the fluid

That means, therefore, this f will not be equal to $f + f_s$ and this f_s is a shifting frequency. This $f + f_s$ may higher than f , may lesser than f , that will depend upon so many things that we will discuss now. But what we can say that the frequency received by the receiver in absence of tracer particle, will not be equal to the frequency received by the receiver in presence of the tracer particle. And this f_s , is nothing but the phase shift and this f_s is known as frequency shift or additional shift or shift in frequency.

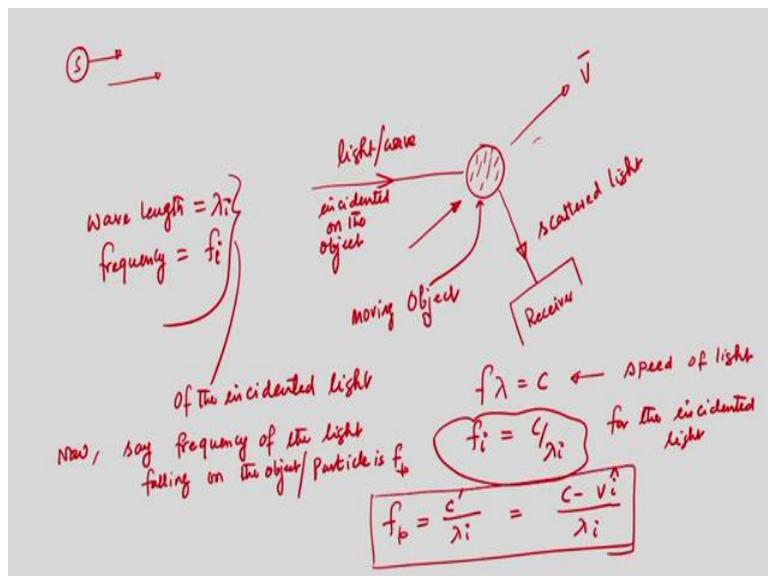
Now, this shifting frequency can be directly correlated, this f_s shift, frequency shift of course, this shift can be directly correlated to the fluid velocity and that is what we will now discuss.

So, that means, what we are using, we are using scattering of light by particle, for which we have a shifting frequency. So, that is the doppler effect and that is how doppler effect is coming into picture, when we talk laser doppler anemometry. So, that means scattering of light by the particles, scattering of lights by the particles and as a result of which phase shift or shift in the frequency I can say, shift in frequency and this is the doppler effect.

So, that is how doppler effect is coming into picture, because what we are doing? We are using the scattering of light by the particle which are seeded in the fluid. And from there we are trying to measure the shifting frequency and from that shifting frequency can be directly correlated to the fluid velocity. Mind it, the particles which are seeded in the fluid are the, are neutrally buoyant, the density of the particle is the density of the fluid. So, the particles are expected that the particle will largely follow the flow direction. And from there, we can correlate the fluid velocity.

So, next we will see how we can now calculate the, you know, that shift and that shift can be correlated with fluid velocity.

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So, if we consider there is a object and our light or wave is incident on that object. So, this is the object and that object say is moving in this direction, with a velocity v. So, the object is moving. So, this is the object, which is moving and light is incident on the object. So, say the light is falling on the object, object is moving v. So, the light will, the object will try to scatter the light and the light scattered lights that is say received by the receiver. So, this is the receiver.

So, this is scattered light. And this is the moving object, and this is light or wave incidented on the object. And if we considered the wave length is λ_i , and frequency is f_i of the incidented light. So, object is moving in the, with the velocity v and light is falling on it having frequency f_i and λ_i and there will be scattering and a scattered light is received by receiver. Now, we know that $f \lambda = c$ that is the speed of the light. Therefore, f_i will be equal to c / λ_i , for this particular case, for the incidented light, that we can write.

So, f_i is equal to c / λ_i , so the, this is what the frequency of the incidented light. Now, particle is moving with a velocity v , so the frequency of the light which is falling on the particles that we need to calculate. So, if we try to calculate, I can write over here. Now, say frequency of the light falling on the object is f_p , say this is f_p on the object of particle, so on the particle or particle f_p . Then, this f_p will be, it should not be c / λ_i , it should be $c / \lambda_i - v$. Because particle is now moving, it is not stationary.

So, the light which is falling on the particle, the light has frequency f_i that is c / λ_i that is what we know, we have assumed the frequency of the light is f_i . Now, the frequency of the light, the frequency received by the receiver in presence of particle. So, the receiver will now receive a frequency and that is f_p and that is $c / \lambda_i - v$. So, if the particle is not there, then the receiver will receive the frequency that is equal to the f_i . But now, because of the presence of the particle which is moving with a velocity v , the receiver will now receive a signal that is f_p that is $c / \lambda_i - v$.

Now, that is nothing but, I can write $c - v$ by λ_i . And, I would like to put an unit vector i over here, because, the particle moment if it is in the direction of light, incoming light and particle both, you know the direction of both the light and incoming light and particles are in the same, then the unit vector will be minus 1. But unit vector will be 1, but if they are in the opposite direction, so the, if the particle moves in the direction from where the light is coming, then the unit vector will be the minus 1 and that will be $c + v$.

So, we can assume as if someone is creating a sound, say someone is creating a sound from this source, so this is source, he is creating a sound and sound wave is coming in this direction and someone is also moving from, you know away from the source and with time what he or she will face that with time the, you know sound waves will be reduced. So, that means, the source and the object, both of them are moving in the same direction. So, that I

mean, source is not moving, then you know light which is coming from the source, the direction of the light and the movement of the object in the same direction.

So, with time then, you know strength of the frequency will reduce and that is the c minus v_i . Now, if they are in the opposite direction that means, if the light is coming from a source and object is also moving towards a source then that will be c plus v_i . So that means, the strength or the frequency will, you know keep on increasing. So, now, this is c minus v_i by λ , so that we can write.

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We need to know λ_p → Wave length of the light fall on the particle
↑ Shift

$$\lambda_p = \frac{c}{f_p} = \frac{(c - \vec{v}_i \hat{i})}{f_p}$$

✓ wave length of the signal when source is moving

$$\lambda_s = \frac{c''}{f_p} = \frac{c - \vec{v}_j \hat{j}}{f_p}$$

$$\lambda_s = \frac{(c - \vec{v}_j \hat{j}) \lambda_i}{(c - \vec{v}_i \hat{i})}$$

Wave length = λ_i
frequency = f_i
of the incident light

Now, say frequency of the light falling on the object/particle is f_p

light/wave incident on the object
moving Object
scattered light
Receiver

$f \lambda = c$ ← speed of light

$f_i = \frac{c}{\lambda_i}$ for the incident light

$$f_p = \frac{c'}{\lambda_i} = \frac{c - \vec{v}_i \hat{i}}{\lambda_i}$$

So, when you know the frequency f_p , then we will like to calculate λ_p . So, this λ_p essentially the first shift, this is the shift. So, λ_p is the frequency, wavelength, λ_p is wavelength we need to know, we need to know λ_p , λ_p . And that is

wavelength of the light, you know fall on the particle, the frequency of the light. So, λ_p will be equal to, you know c by f_p using that relationship. Now, if I plug in the value of c by f_p that is, c into λ_i divide by, you know c minus v into unit vector. So, this v is vector. So, this is v and so, this will be unit vector. So, this is λ_p .

Now, so that means, now object a light is falling on the object, object will try to scatter, object is moving in the direction, you know with a velocity v . So, we will get a frequency and that is what we have calculated and we have calculated wavelength. Now, if the frequency of the incident light, rather if the source is moving, so now, we need to receive a signal by the receiver when, as if the object is moving. Now, the light that will be transmitted by the, you know kind of I can say, so this is λ_p .

Now, the particle is moving with the fluid. So, the particle velocity is equal to the fluid velocity, light is falling on it, it will scatter light and we have calculated wavelength of the light fall on the particle λ_p .

Now, the light is now moving, the object is now moving, as if now we will received the, a signal from the object by the receiver. So, now object is moving as if the source is moving, in that case what will happen. So, if, the wavelength of the signal when source is moving. So, now question is as if the light is, you know incidented on the particle, particle will scattered and we have calculated the frequency, the wavelength of light fall on the particle λ_p that is c by f_p . If there is no particle, the receiver will receive f_i that is λ .

Now, the wavelength which is falling on the particle is λ_p , but wavelength that will be received by the receiver when particle is present that is λ_s and that is again, c double prime, say c double prime by f_p . This c double prime again it is c minus v_j , I again do not know where, because again I am using the unit vector j . And again, we can apply the same argument if the, if the direction are in the same direction, if they are in the same direction, j will be plus 1.

If they are of, you know approaching towards them, then it will be minus 1. So, c minus v_j by f_p . And if I put the value of f_p from the previous equation, then λ_s will be equal to, rather I can write c minus v_j λ_i by c minus v_i .

So, this is the expression of the λ_s , when source is moving. Again, I am telling when there is no particle, receiver will receive a signal that frequencies of high, when the particle is there, because of the moment of the particle, the wavelength which is falling on the light, on

this is the, you know, incidented and this is how much light scattered. And, this f_D if you do algebraic manipulation, we can write.

This is nothing but, c into c minus v_i divide by λ_i into c minus v_j minus f_i is equal to c by λ_i . So, if I take now, c by λ_i out, then we can write c minus v_i minus c plus v_j these are the unit vectors by, c minus v_j . So, this is c by λ_i into v_j minus v_i , by c minus v_j .

So, ultimately, we can write f_D that is doppler shift, is v_j minus v_i c by λ_i by c minus v_j . So, you can see the doppler's, that is you have written over here the doppler effect. Now, the change in frequency can be directly correlated, that is f_s that is what we have, you know discussed at the beginning of this class, that doppler effect, the shift in frequency that can be correlated with the fluid velocity.

Now, in most of the applications, the you know most of the application I can say, almost for all the applicants, if I write that light intensity of the laser, I mean v the velocity of the fluid is much, much less than c that is true for almost all the applications, for all the applications.

If that is the case, then f_D is equal to, I can write c by λ_i v_j minus v_i divide by c . So, this is equal to v into j minus v into i divide by λ_i . So, we can see that the doppler shift that is what we told at the, rather in the beginning of this course, this doppler shift, doppler effect. Shift in frequency, shift in frequency is directly related to the fluid velocity. So that means, f_D is proportional to v function velocity. So, what we can say, that means, we have discussed light is incidented on object, if there is, there is no particle, the signal received by the receiver will be f_i .

In presence of particle, which are tracer particle which are neutrally buoyant, density is equal to the fluid density that means, the particles are following the, you know bulk flow. Now, in that case, if the light is incidented on the particle, the light will be scattered by the particle. In that case, we have calculated the frequency of the light which is falling in the particle. And, now source is moving, in that case the signal received by the receiver again we have calculated by f_s .

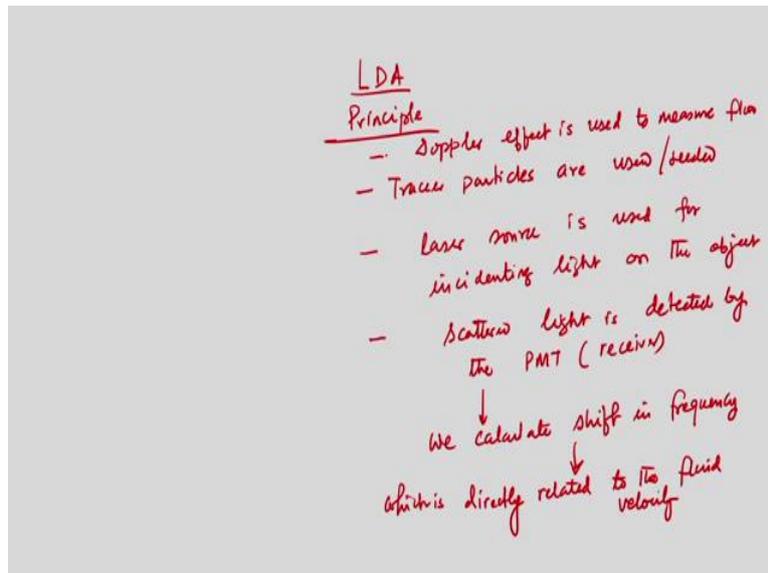
So, now, f_s minus f_i , that is nothing but the doppler effect that we have calculated, and we have seen that the doppler effect that is shift in frequency that can be, you know captured by the receiver, receiver is nothing but, you know photomultiplier tube. So, this receiver we have, you know shown in the schematic, the receiver is essentially photomultiplier tube. So,

when light is received by this photomultiplier, the photo it absorbed photo energy and that energy is getting converted to the current and from there we can calculate the frequency. So, this photomultiplier tube, photo multiplier tube.

So, this is the receiver. So, it receives photon, that energy is converted to the current and from there we calculate frequency. So, now by calculating the frequency from the receiver, we can directly correlate to what will be the velocity of the fluid.

So, this is what is the basic principle of the LDA technique, the mathematical analysis that we have done, that is not particular. This is a genetic analysis, this is valid almost for all the light (())(46:27) based technique. Now, to summarize what we have discussed today, that is very important that I can write for the sake of completeness, that principle.

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So, LDA, the principle that is tracer particle, tracer particles are used or seeded, doppler effect is used to measure flow, flow velocity measurement that is point velocity measurement. Laser source is used for incidenting light on the object. Scattered light is detected by the PMT or receiver photo multiplier tube and we calculate shift in frequency, and this shift in frequency is, which is directly related to the fluid velocity. So, this is the basic principle of using laser doppler anemometer to measure the flow velocity that is the point velocity.

We have discussed that flow measurement is the volumetric flow measurement, point velocity measurement and the determination of the flow streamlines. We have discuss about the techniques which are used to measure volumetric flow rate, we have discuss about the

techniques which is used to measure point velocity that is hot wire and hot film and today we have discuss about LDA. And today we have discuss, about the basic principle by which we can measure flow velocity and we have seen this is completely a noninvasive technique and which is used in situation where fluid is corrosive, acidic and flow is highly contaminated.

And since, this is not immersed or this is not placed in the flow field, they do not disturb the flow field and as a result, the measurement which we are obtaining using this technique is almost accurate one. So, today, we have discussed about another important technique, which is used to measure the velocity at a point.

And we have discuss, about the basic principles with small, you know mathematical analysis that, how you can calculate the flow velocity, rather how you can calculate velocity in with the frequency of the light which is falling on the object. So, with this I stop my discussion today and we will continue my discussion next class. Thank you.