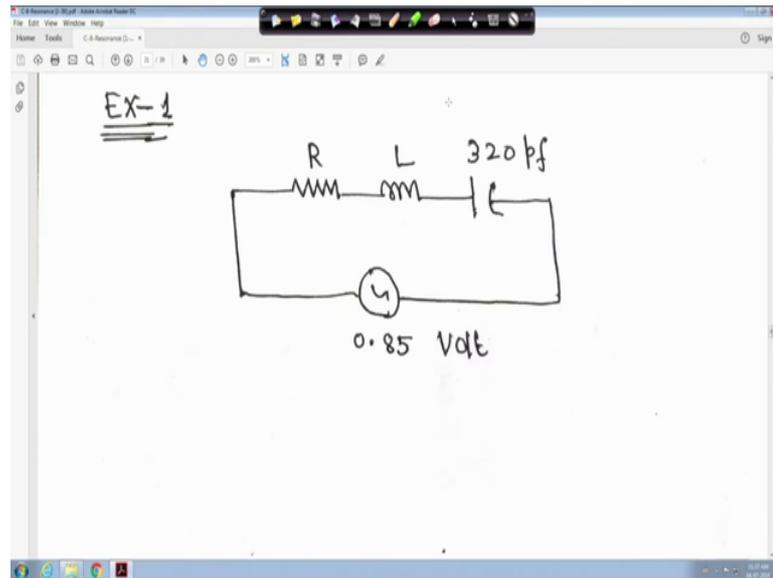


Fundamentals of Electrical Engineering
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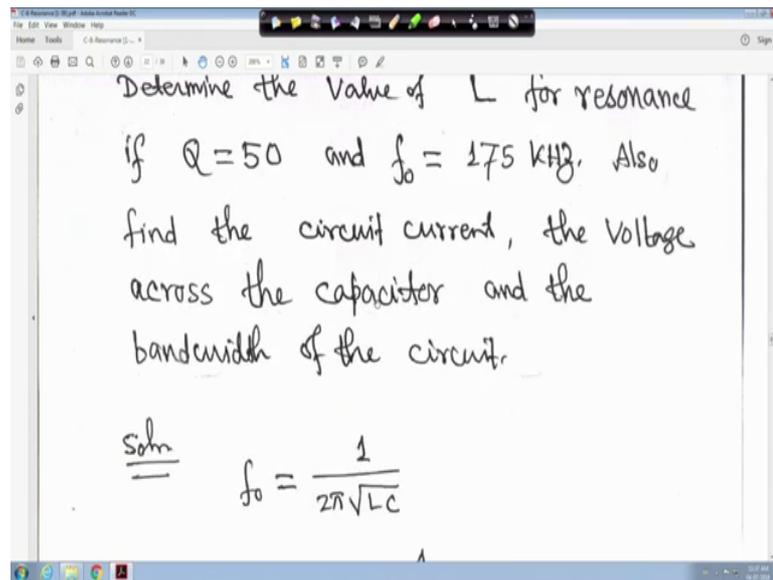
Lecture – 46
Resonance and Maximum Power Transfer Theorem (Contd.)

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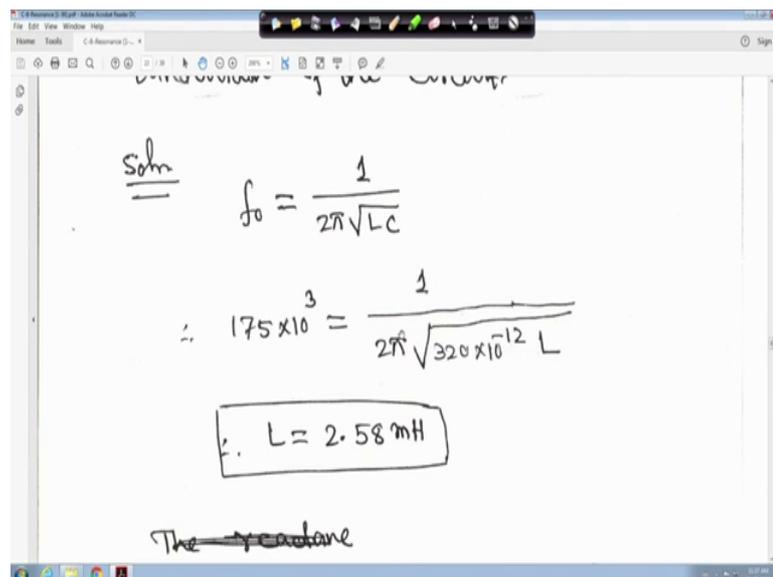
So, far what whatever little bit theories are there for resonance we have seen it. Now, we will take a simple example right. So, this is a simple series RLC circuit. This is R L is given, and this is 320 peak of farad. And if you want this instantaneous polarity, you can take plus minus, and this voltage is 0.85 volt right. So, this will be RLC circuit what we have to do it. So, it is written in it.

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So, this is example L that you have to determine the value of L for your what we call for resonance if Q is equal to 50 right and f_0 is equal to 175 kilo hertz. Also find the circuit current, the voltage across the capacitor and the bandwidth of the circuit right. So, this is the problem, this is the circuit, this is the circuit, and this is the what we have to determine everything is given here right.

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So, first thing we know that resonance frequency f_0 is equal to 1 upon 2 pi root over LC . So, f_0 is given 175 kilo hertz. So, it is 175 into 10 to the power 3 is equal to 1 upon 2 pi

root over your what we call C is given 320 peak of farad, 320 into 10 to the power 12 into L from which you will get L is equal to 2.58 milli Henry right.

(Refer Slide Time: 01:27)

The handwritten notes show the following calculations:

$$X_L = L\omega = 2.58 \times 10^{-3} \times 2\pi \times 175 \times 10^3 \text{ } \Omega$$

$$\therefore X_L = 2840 \text{ } \Omega$$

Since $Q = \frac{\omega_0 L}{R}$

$$\therefore R = \frac{\omega_0 L}{Q} = \frac{175 \times 10^3 \times 2.58 \times 10^{-3}}{50}$$

$$\therefore R = 56.8 \text{ } \Omega$$

Now, we know that X_L is equal to $L\omega$, so L we have got it 2.58 into 10 to the power minus 3 right, it is in Henry into your 2 pi into f_0 is equal to 175 into 10 to the power 3 hertz right so that means X_L is equal to $L\omega$, this much of ohm. So, it is 2840 ohm right. So, quality factor Q is equal to $\omega_0 L$ upon R right. So, $\omega_0 L$ your a your what you call this $\omega_0 L$ that means R is equal to $\omega_0 L$ upon Q right.

(Refer Slide Time: 02:04)

The handwritten notes show the following calculations:

The impedance of the circuit at resonance is (23)

$$Z = R = 56.8 \text{ } \Omega$$

$$\therefore I_0 = \frac{V}{R} = \frac{0.85}{56.8} = 14.96 \text{ mA}$$

Also

$$V = \frac{I_0}{\omega C} = \frac{RI_0}{\omega C}$$

So, here you just substitute or substitute your all these values. So, you will get your R is equal to 56.8 ohm right. So, this way actually your L we have got that is your 2.58 milli Henry. And you if your f_0 is given this one right $2\pi f_0$ one thing is there, one correction is there. Here it is your ω_0 your ω_0 is equal to $2\pi f_0$ right, I think one 2π is missing right. Just check this answer I think this answer is correct, perhaps this I missed this one, it will be ω_0 right.

So, Q is equal to your 50, Q is equal to 50 is given, R is equal to $\omega_0 L$ upon this thing. This you please check it right hope this is correct. So, next this one R you have got then the impedance of the circuit of the resonance is that that at resonance X_L is equal to X_C , so Z is equal to R it is 56.8 ohm. So, I_0 is equal to V upon R, so V is given 0.85 volt divided by R, so 14.96 milli ampere right.

So, also V C is equal to I_0 upon $\omega_0 C$, so this means it is R I_0 by numerator and denominator you multiply by R, R I_0 upon $\omega_0 C R$, so that means, V C is equal to Q V right. So, that means, if you your what you call you know that your R I_0 is equal to your what you call R I_0 is equal to V and $\omega_0 C R$ that is 1 upon ω_0 your C R is equal to Q, so it will be Q into V right. Therefore, voltage across the capacitor will be 50 into 0.85; V is 0.85 volt, and Q is 50, so 42.5 volts.

(Refer Slide Time: 03:58)

Voltage across the capacitor
 $= QV = 50 \times 0.85 = 42.5 \text{ Volt.}$

Bandwidth, $= (\omega_2 - \omega_1)$

~~$Q = \frac{\omega_0}{\omega_2 - \omega_1}$~~

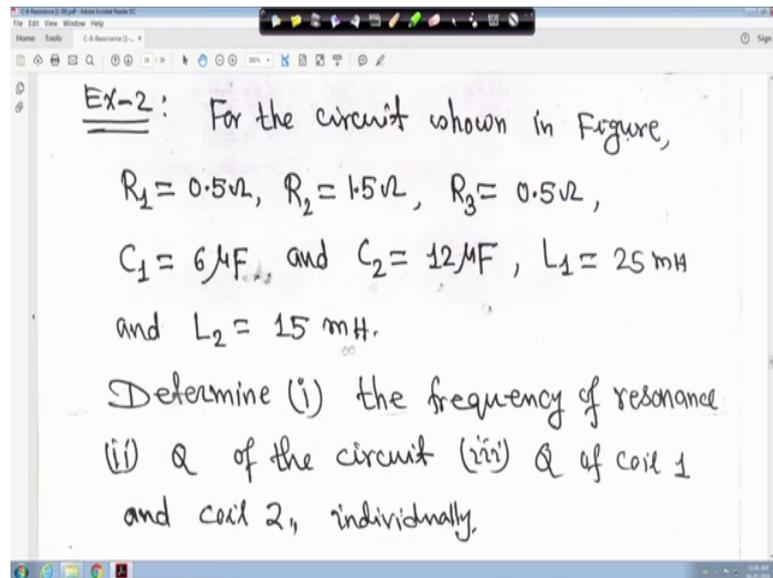
$Q = \frac{\omega_0}{\omega_2 - \omega_1} = \frac{f_0}{f_2 - f_1} = \frac{f_0}{BW}$

$\therefore BW = \frac{f_0}{Q} = \frac{175 \times 10^3}{50} = 3.5 \text{ kHz}$

And bandwidth is ω_2 minus ω_1 or it is radian per second or f_2 minus f_1 in hertz right. So, Q you know we have derived this Q is equal to ω_0 by ω_2

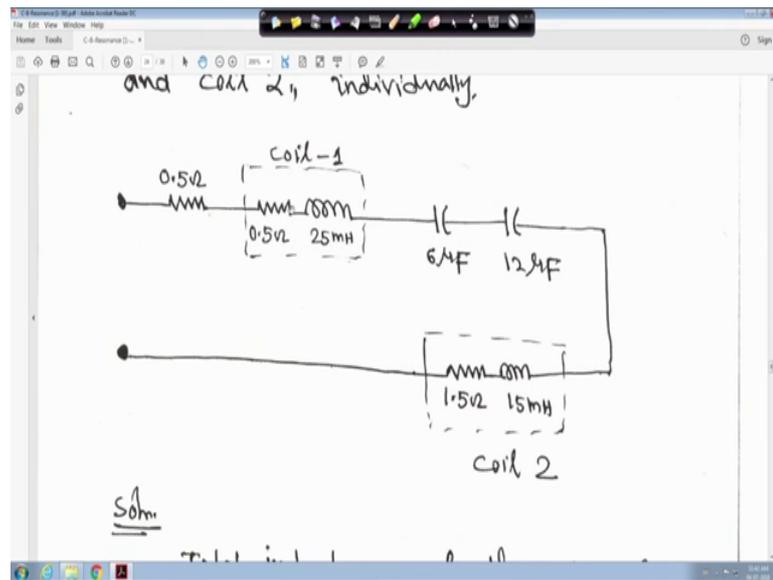
minus ω 1 is equal to you can write f_0 upon f_2 minus f_1 is equal to f_0 by bandwidth. Therefore, bandwidth is equal to f_0 by Q . When you take in terms of f_0 , it is in hertz, so 175 into 10 to the power 3 divided by Q is equal to 50 , so 3.5 say kilohertz right, so bandwidth.

(Refer Slide Time: 04:51)



Now, example 2 so, this is simple example right, only thing is that this your what you call here I told you just (Refer Time: 04:35) ω_0 is actually 2π into f_0 , I might have missed 2π , just check the answer right whether it is 2π is taken care or not right, so it is (Refer Time: 04:45) 56.8 just check. So, this one your next is for the circuit shown in figure that R_1 is equal to I will show you the circuit R_1 is given 0.5 ohm, R_2 1.5 ohm, and R_3 is equal to point ohm; C_1 6 microfarad, and C_2 12 microfarad, L_1 25 milli Henry, and L_2 15 milli Henry. So, determine the frequency of the resonance that is first one; second one, Q of the whole circuit; and 3 Q of coil 1 and Q of coil 2 individually.

(Refer Slide Time: 05:15)



So, this is my series circuit, this is resistance is given 0.5 ohm. This is coil 1, its resistance is 0.5 ohm, inductance is 25 milli Henry. These two capacitors are there in series 6 microfarad, and 12 microfarads right. And this is the coil 2, resistance is 1.5 ohm, and inductance is 15 milli Henry. This is the problem. So, now question is impedance of the circuit. So, L this the your 25 milli Henry, and 15 milli Henry find out the total equivalent your what you call L. So, it is 25 plus 15 means 40 milli Henry right. And these two capacitor are in series means it is equivalent to the view obtain the resistance series in parallel. So, it will be 6 into 12 by 6 plus 12 right, so this will be 4 microfarad.

(Refer Slide Time: 05:59)

coil 2

Soln.

Total inductance of the circuit

$$L = (25 + 15) = 40 \text{ mH}$$
$$\text{Total } C = \frac{6 \times 12}{(6 + 12)} = 4 \mu\text{F.}$$

So, C is equal to 6 into 12 upon 6 plus 12 is equal to 4 micro Farad. And then R your what you call we know that f_0 is equal to $\frac{1}{2\pi\sqrt{LC}}$. It is 1 upon 2 pi (Refer Time: 06:11) 40 milli Henry. So, 40 into 10 to the power minus 3 into 4 into 10 to the power minus 6, the capacitor 4 micro farad; so, these actually will get f_0 is equal to 10 to the power 4 by 8 pi hertz by your 8 pi hertz or ω_0 is equal to 2.5 into 10 to the power 3 radian per second either you have hertz or radian per second right.

(Refer Slide Time: 06:34)

(25)

$$\therefore f_0 = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{40 \times 10^{-3} \times 4 \times 10^{-6}}}$$
$$\therefore f_0 = \frac{10^4}{8\pi} \text{ Hz.} \quad \text{OR} \quad \omega_0 = 2.5 \times 10^3 \text{ rad/sec.}$$
$$Q \text{ of the circuit} = \frac{L\omega_0}{R}$$
$$= \frac{2.5 \times 10^3 \times 40 \times 10^{-3}}{2.5} = 40$$

So, now Q of the whole circuit it will be $L \omega_0$ upon R right. So, L we have got your what you call that wherever your this thing (Refer Time: 06:42). This is your L 40 into 10 to the power minus 3 whole circuit this is correct 2.5 into 10 to the power minus 3 10 to the power 3 radian per second is equal to actually this will become 40 is equal to 40. So, this is not there right. This is my class note, so all corrections made actually same thing I have scanned it here for you right.

So, this is 40 right. So, this is correct, therefore this is not twisting. This is actually 40 it is written here correct this is 40 here right. So, Q of the whole circuit is 40 right. So, let me clear it. So, then this one that Q of coil 1 it is $L_1 \omega_0$ upon R_1 for the coil ω_0 is 2.5 into 10 to the power your what you call this ω_0 is equal to 2.5 into 10 to the power 3 radian this thing your what you call it is radian per second it is given here ω_0 .

(Refer Slide Time: 07:35)

The image shows a digital whiteboard with handwritten mathematical derivations. At the top, there is a calculation: $\frac{2.5}{2.5} = 125$. Below this, the quality factor Q of the whole circuit is given as $Q = 125$ with a checkmark. The derivation for the Q of coil 1 is shown as $Q \text{ of coil 1} = \frac{L_1 \omega_0}{R_1} = \frac{25 \times 10^{-3} \times 2.5 \times 10^3}{0.5} = 125$. The derivation for the Q of coil 2 is shown as $Q \text{ of coil 2} = \frac{L_2 \omega_0}{R_2} = \frac{15 \times 10^{-3} \times 2.5 \times 10^3}{1.5} = 25$.

And L 1 is equal to your this one L 1, here L 1 is equal to actually this one 25 milli Henry right. So, here your here this one it will be your let me correct it will be L 1 is equal to 25 not 2.5 right. So, in this case this answer is 12.5 it will be actually 125 right. So, just check just check it will let me let me make it half right. So, it is 25, so, this is cancelled right, and this is 2.5, so answer will be 125 right. So, this is not 12.5, because it is 25 milli Henry by mistake I took it. This is my class note everything it is corrected actually right. So, similarly L 2 ω_0 , L 2 15 milli Henry, and your that is 15 into 10 to the

power minus 3, and it will be omega 2.5 into 10 to the power 3 upon R 2 is equal to 1.5 right.

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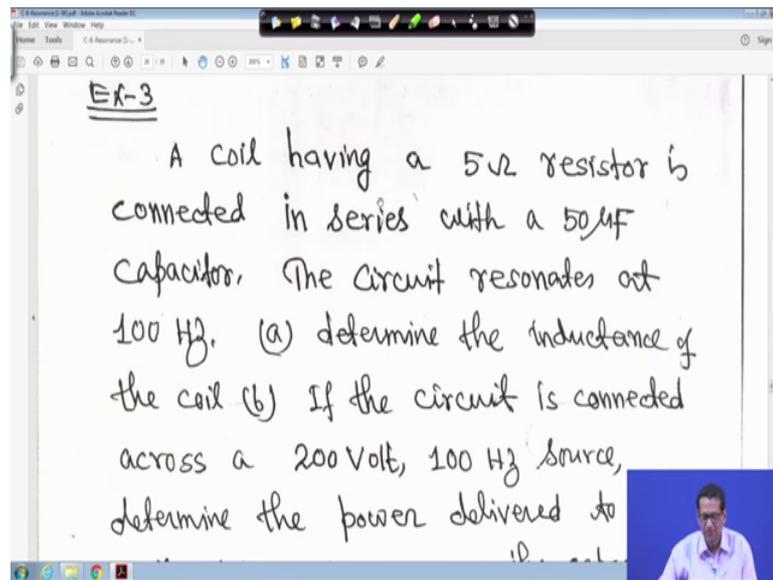
$$= 25$$

$$BW = \frac{f_0}{Q} = \frac{10^4}{8\pi \times 25} \text{ Hertz} \approx 10 \text{ Hz}$$

If you calculate it right, so just if we calculate it, it will be 25. So, please check all these squares then by little bit it will be calculation all these three please do it of your own right, see that all calculations are correct. So, bandwidth is we know we have done it band width is equal to f_0 upon Q right. So, your what you call you substitute or you substitute your all this thing f_0 is equal to we have got it 10 to the power 4 upon 8 pi hertz.

So, here it is 10 to the power 4 upon 8 pi, and Q is equal to whatever you have got right, Q is equal to your over overall thing is 40. This Q we got is 40 right this 40. So, it is corrected here it is 40 right. So, if you do it approximately, it will become 10 hertz right. So, this is the bandwidth this is not 25, this is 40, because you got this is 40. So, this will be approximately 10 hertz. So, this is one.

(Refer Slide Time: 09:30)



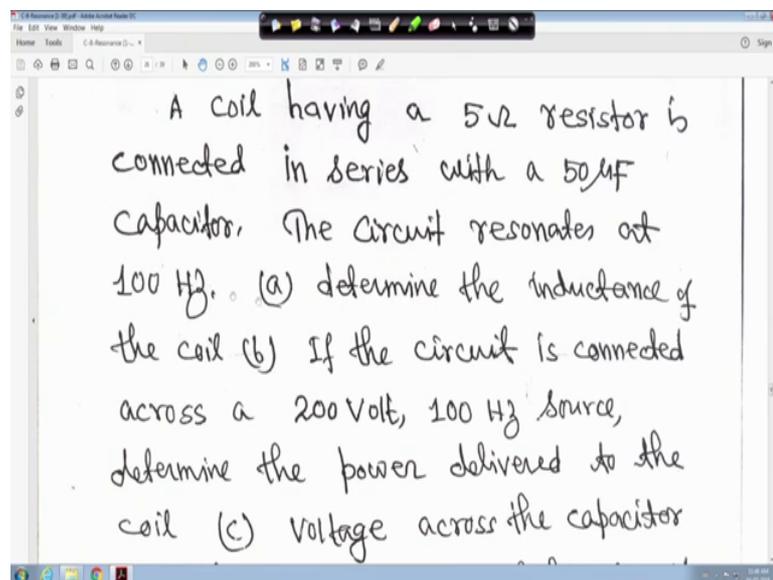
The image shows a digital whiteboard with a handwritten problem statement. The text is written in black ink on a white background. The problem is titled "Ex-3" and describes a series RLC circuit. It asks for the inductance of the coil, the power delivered to the coil, and the voltage across the capacitor.

Ex-3

A coil having a 5Ω resistor is connected in series with a $50\mu\text{F}$ capacitor. The circuit resonates at 100 Hz . (a) determine the inductance of the coil (b) If the circuit is connected across a 200 Volt , 100 Hz source, determine the power delivered to the coil (c) voltage across the capacitor

So, another one is example 3. A coil having a 5 ohm resistor is connected in series with a 50 micro farad capacitor.

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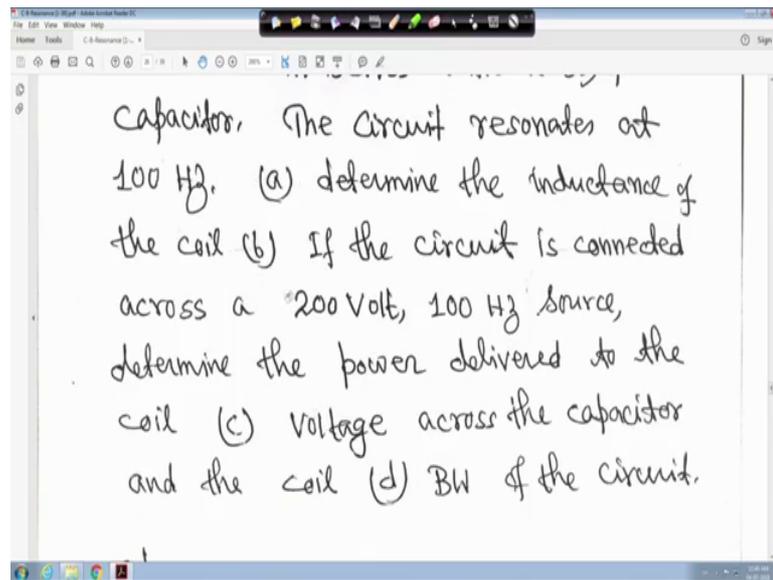
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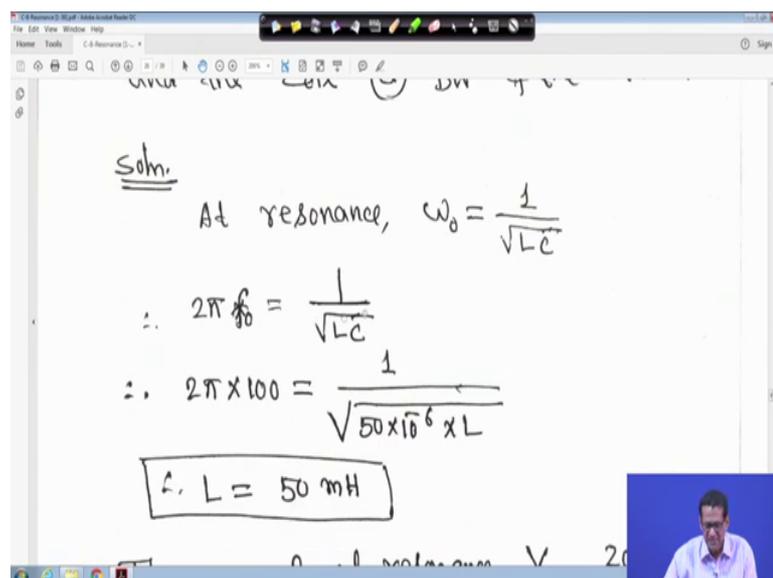
The circuit resonates at 100 hertz that means your f_0 is equal to 100 hertz ; a, determine the inductance of the coil; b, If the circuit is connected across a 200 volt 100 hertz source, determine the power delivered to the coil.

(Refer Slide Time: 09:49)



And c, now the last one (Refer Time: 09:54) voltage across the capacitor and the coil, voltage of the capacitor and the coil, and d is the bandwidth of the circuit. This is the thing you have to find it. When you read this video lecture, first you note it down right, then you solve the problem. So, you are what you call, so circuit you can do of your own circuit is not drawn it is very simple thing right. So, at resonance ω_0 is equal to 1 upon root over $L C$ that you know.

(Refer Slide Time: 10:19)



So, $2\pi f_0$ is equal to 1 upon root over $L C$. So, f_0 is given 100 hertz.

(Refer Slide Time: 10:24)

$$\therefore 2\pi \times 100 = \frac{1}{\sqrt{50 \times 10^{-6} \times L}}$$
$$\therefore L = 50 \text{ mH}$$

The current at resonance $\frac{V}{R} = \frac{200}{5} = 40 \text{ Amp}$

And C is given 50 micro farad, so 50 into 10 to the power minus 6 farad and it is L. So, L will become (Refer Time: 10:30) is 50 milli Henry. Now, the current at resonance will be V upon R, because X L is equal to (Refer Time: 10:37). So, the current is maximum so 200 by 5, so current is 40 ampere right. Now, power dissipated in I square R, so 40 square into 5 8000 Watts is equal to 8 kilo watt right.

(Refer Slide Time: 10:51)

$$\text{power dissipated} = (40)^2 \times 5 = 8000 \text{ Watts,}$$
$$= 8 \text{ kW.}$$
$$\text{Voltage across capacitor} = I X_c$$
$$= \frac{40}{50 \times 10^{-6} \times 2\pi} = 800 \text{ Volt}$$

So, voltage across this capacitor voltage across capacitor magnitude I X C right so, I is 40 ampere, and X C is equal to 1 upon omega C, C is equal to 50 micro farad. So, 50 into

10 to the power minus 6 farad into 2 pi into 100. So, it comes around 8000 by 2 pi volt right. Approximately this is this is your 1273.2 volt. This is this is not this thing, this is the correct one 1273.2 volt right.

(Refer Slide Time: 11:25)

$$= 127.32 \text{ Volt} \Rightarrow 1273.2 \text{ V.}$$

The Impedance of the coil

$$= R + jL\omega$$

$$= 5 + j 50 \times 10^{-3} \times 2\pi \times 100 = (5 + j 31.4) \Omega$$

$$V_L = 40 \times (5 + j 31.4) = 1256 \text{ V}$$

So, the impedance of the coil R plus j L omega so, it is 5 plus j L is 50 into 10 to the power minus 3 into 2 pi into 100 right. So, it is 5 plus j 31.4 ohm. So, V L is equal to I into your Z, so this is 40 is the current we have got into this jth you will get its magnitude it 12 your 1256 volt we have taken magnitude only that your what you call this an angle is not written here right. So, our interest magnitude only, so this one actually it will be multiplied by 40 you just check it right, and root over 5 square plus 31.4 square whatever it comes just check it will be 1256 volt right.

Only magnitude written here, this is actually if I make it, I should make it bar (Refer Time: 12:14) taken here 1256 volt right. So, now Q of the coil will be is equal to your what you call it will be 31.4 by 5 right, because it is X L is 31.4 right and R is 5, so it is 6.3 right. It is a it is basically your what we call the Q 0 of the coil. So, it is X L X L is basically the L omega by R.

(Refer Slide Time: 12:42)

The screenshot shows a digital whiteboard with the following handwritten text:

$$V_L = \cancel{40} \cdot 40 \times (5 + j31.4) = 1256 \text{ Volt}$$
$$Q_0 \text{ of the coil} = \frac{31.4}{5} = 6.3$$
$$BW = \frac{f_0}{Q_0} = \frac{100}{6.3} = 16 \text{ Hz}$$

A small video inset in the bottom right corner shows a man in a white shirt speaking.

So, $L\omega$ is actually 31.4 divided by R is 5, so 6.3. And bandwidth is equal to f_0 upon Q_0 100 upon 6.3 is equal to 16 hertz right. So, this is the simple thing,

(Refer Slide Time: 12:55)

The screenshot shows a digital whiteboard with the following handwritten text:

(28)

Ex-4: A series circuit with $R = 50 \Omega$,
 $L = 0.05 \text{ H}$ and $C = 20 \mu\text{F}$ has an applied
voltage $V = 100 \angle 0^\circ$ Volt with a
variable frequency. Find the maximum
voltage across the inductor as the
frequency is varied.

A small video inset in the bottom right corner shows a man in a white shirt speaking.

Now, example 4, a series circuit with R is equal to 50 ohm, L is equal to given 0.05 Henry, C is 20 micro farad has an applied voltage V is equal to 100 angle 0 volt with a variable frequency. Frequency is variable here. Find the maximum voltage across the inductor as the frequency is varied. You have to find out the maximum voltage right across the inductor as the frequency is varied. Now, now Z is equal to root over R square

plus $L\omega$ minus $\frac{1}{\omega C}$ upon ωC square that is X_L minus X_C square. Therefore, current I is equal to magnitude V upon magnitude of the current root over R square plus $L\omega$ minus ωC square whole square right.

(Refer Slide Time: 13:34)

Soln.

$$Z = \sqrt{R^2 + \left(L\omega - \frac{1}{\omega C}\right)^2}$$

$$I = \frac{V}{\sqrt{R^2 + \left(L\omega - \frac{1}{\omega C}\right)^2}}$$

Magnitude of the voltage across L is

$$V_L = I(L\omega) = \frac{\omega L V}{\sqrt{R^2 + \left(L\omega - \frac{1}{\omega C}\right)^2}}$$

So, magnitude of the voltage across L V_L will be I into $L\omega$ (Refer Time 13:39) magnitude so that means, X_L is accelerating I into X_L , so X_L is equal to $L\omega$. So, it will be $\omega L V$ upon root over R square plus $L\omega$ minus ωC whole square.

(Refer Slide Time: 13:52)

$$V_L = I(L\omega) = \frac{\omega L V}{\sqrt{R^2 + \left(L\omega - \frac{1}{\omega C}\right)^2}}$$

Setting the derivative $\frac{dV_L}{d\omega}$ of eqn. (1) equal to zero and solving for ω , we obtain the value of ω when V_L is a maximum

So, setting the derivative dV_L upon $d\omega$ you take the derivative of this equation 1 with respect to ω right. So, and what you call is equal to 0, and solve for a ω we obtain the value of ω when V_L is maximum right, so that means, dV_L upon $d\omega$ is equal to this one. It is simplified and written to the power minus half you please do little bit of your own. I mean what is there this your X_L minus ω square it is expanded right.

(Refer Slide Time: 14:08)

$$\frac{dV_L}{d\omega} = \frac{d}{d\omega} \left[\omega L V \left(R^2 + \omega^2 L^2 - \frac{2L}{C} + \frac{1}{\omega^2 C^2} \right)^{-\frac{1}{2}} \right] \quad (29)$$

$$\therefore R^2 - \frac{2L}{C} + \frac{2}{\omega^2 C^2} = 0$$

$$\omega = \frac{1}{\sqrt{LC}} \sqrt{\frac{2}{2 - R^2 C}} \quad (2)$$

And put your square root here, so 2 to the power minus half right, because it is your ω V upon root over this one, so minus 1 upon R , then you take the derivative. If you derivate and simplify, you will get R square minus 2 L upon C plus 2 upon ω square C square is equal to 0 you will get it that means ω is equal to 1 upon root over $L C$ into root over 2 upon 2 minus R square C upon L right.

(Refer Slide Time: 14:47)

The screenshot shows a digital whiteboard with the following handwritten content:

$$\therefore \omega = \frac{1}{\sqrt{LC}} \sqrt{\frac{2}{2 - \frac{R^2 C}{L}}} \quad \text{--- (2)}$$

Since $Q_0 = \frac{\omega_0 L}{R} = \frac{1}{\omega_0 C R}$

$$\therefore Q_0^2 = \frac{L}{R^2 C} \quad \text{--- (3)}$$
$$\therefore \frac{R^2 C}{L} = \frac{1}{Q_0^2} \quad \text{--- (4)}$$

A small video inset of the presenter is visible in the bottom right corner of the whiteboard.

But, we know we have derived it that Q_0 is equal to $\omega_0 L$ upon R that we have done is equal to you know 1 upon $\omega_0 C R$ that also we have done. And if we also we are if we multiply Q_0 into Q_0 , you will get Q_0 square is equal to 1 upon R square C this also we have derived, this also we have derived that means, these term is the reciprocal of this one R square C upon L is equal to 1 upon Q_0 square. So, here you put 2 minus it will be 1 upon Q_0 square right.

(Refer Slide Time: 15:21)

The screenshot shows a digital whiteboard with the following handwritten content:

$$\therefore \frac{1}{L} = \frac{Q_0^2}{R^2 C}$$
$$\therefore \omega = \frac{1}{\sqrt{LC}} \sqrt{\frac{2}{2 - \frac{1}{Q_0^2}}}$$
$$\therefore \omega = \frac{1}{\sqrt{LC}} \sqrt{\frac{2Q_0^2}{(2Q_0^2 - 1)}} \quad \text{--- (5)}$$

Eqn.(5) shows that for high Q the maximum voltage across

A small video inset of the presenter is visible in the bottom right corner of the whiteboard.

This all this thing we derived so, that means by omega will be is equal to after upon substitution 1 upon root over L C 2 Q 0 square upon 2 Q 0 square minus 1. So, equation 5 shows that for a high Q the maximum voltage your across L occurs at your this omega 0 approximately 1 upon root over L C. Q is very high if Q is very high, then 2 Q 0 square right your what you call minus 1 approximately 2 Q 0 square right. So, this one after Q 0 is very high, so this term will become unity, in that case if it is omega upon oh sorry 1 upon root over L C, so that is your approximate value 1 upon root over L C.

(Refer Slide Time: 16:02)

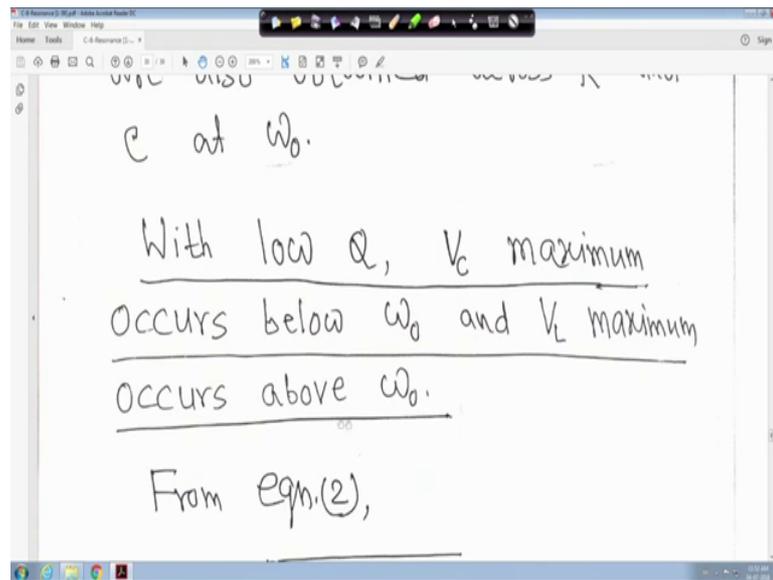
(30)

$$\omega_0 \approx \frac{1}{\sqrt{LC}}$$

If Q is high, Maximum Voltage are also obtained across R and C at ω_0 .

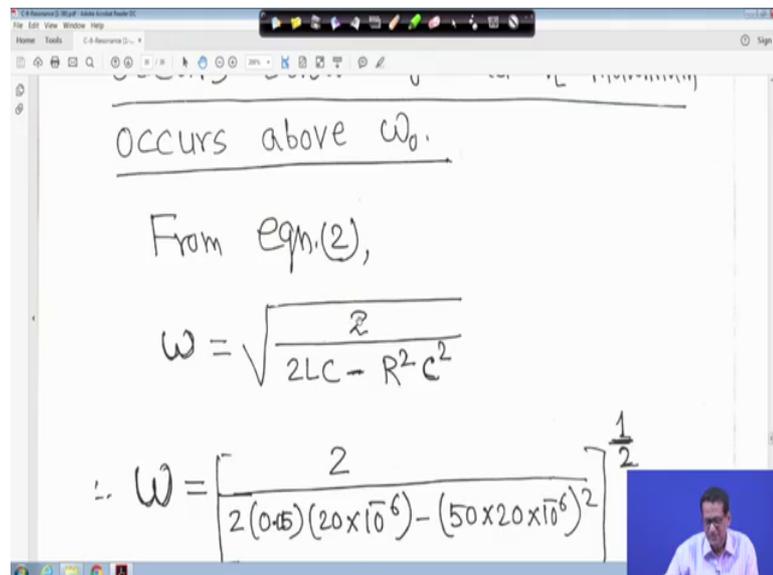
Now, if Q is high, maximum voltage are also obtained across R and C at omega 0 that is your resonance frequency right.

(Refer Slide Time: 16:17)



So, with low Q, V C maximum occurs below omega 0, and V L maximum occurs above omega 0. This is a small exercise to you. You look at this expression and with low Q, V C maximum occurs below omega 0, and V L maximum occurs at above omega 0 this one exercise small exercise for you right. Already we have done it for resonance.

(Refer Slide Time: 16:34)



Now, from equation 2, so omega is equal to you can simplify writing root over 2 upon 2 L C minus R square C square then from this equation that is from your from this equation from this equation, now this is equation 2. From equation 2 we can write like

this. So, you can write like this. So, C R L all values are given you substitute all this value. Everything is given you will get omega is equal to 1414 radian per second this is the answer right. When you take d V L upon d omega is equal to 0, this is the answer right for which voltage across the inductor will be maximum right. So, so X L is equal to L omega 70.7 ohm, X 0 is equal to X C is equal to 1 upon omega C 35.4 ohm please calculate all these things.

(Refer Slide Time: 17:22)

$$X_L = L\omega = 70.7 \Omega$$

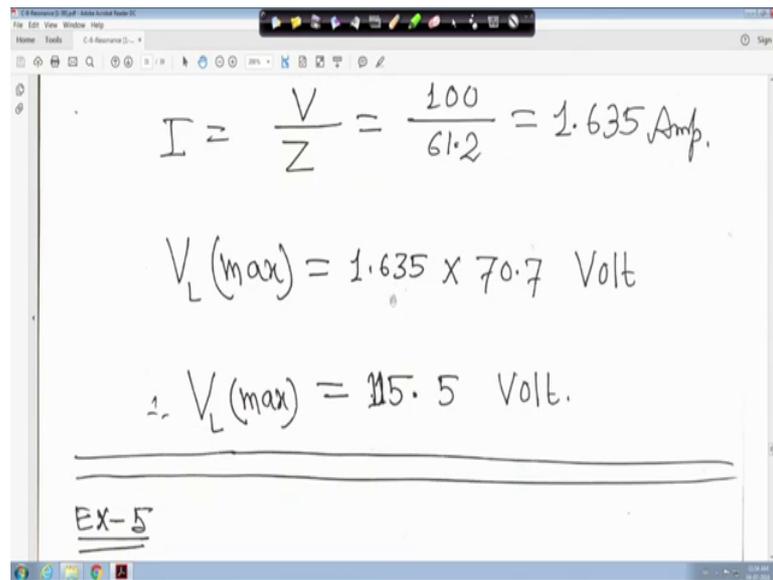
$$X_C = \frac{1}{\omega C} = 35.4 \Omega$$

$$Z = 50 + j(70.7 - 35.4)$$

$$\therefore Z = 61.2 \angle 35.3^\circ \Omega$$

And Z will be then R plus j your X L minus X C. So, whatever it comes it is 61.2 angle 35.3 degree ohm right. Therefore, I is equal to V by Z we get the magnitude that is 100 angle 61.2, so 1.635 ampere right. So, this all these things you please calculate direct substituted for getting omega right. So, it just make this calculation. Therefore V L max will be I into your X L that is your what you call that is your 70.7 right.

(Refer Slide Time: 17:53)



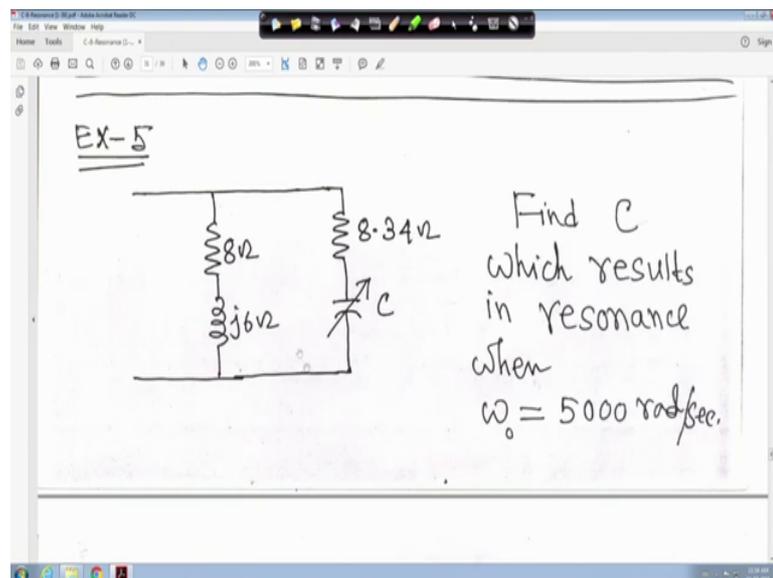
The image shows a digital whiteboard with the following handwritten calculations:

$$I = \frac{V}{Z} = \frac{100}{61.2} = 1.635 \text{ Amp.}$$
$$V_L(\text{max}) = 1.635 \times 70.7 \text{ Volt}$$
$$\therefore V_L(\text{max}) = 115.5 \text{ Volt.}$$

Below the calculations, the text "EX-5" is written and underlined.

So, you get 115.5 volt. This example is very interesting one right. So, this is the VL max.

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So, example 5 in this case this parallel circuit is there. This is an inductive circuit, so 8 plus $j6$ ohm. And this is your capacitive circuit 8.34 ohm, but this C is varying $C \times C$ varying. You have to find C , which results in a resonance ω_0 is equal to 5000 radian per second right. So, in this case this problem is very simple, because ω_0 is given. So, in the parallel circuit; so, Y is equal to 1 upon 8 plus $j6$ plus 1 upon 8.34 minus jXC right.

(Refer Slide Time: 18:32)

The image shows a handwritten derivation for admittance Y . At the top right, the number 32 is circled. The derivation starts with the equation $Y = \frac{1}{8+j6} + \frac{1}{8.34-jX_C}$. This is followed by the simplified form: $\therefore Y = \left(\frac{8}{100} + \frac{8.34}{69.5+X_C^2} \right) + j \left(\frac{X_C}{69.5+X_C^2} - \frac{6}{100} \right)$. Below this, it says "At resonance" and then the equation $\frac{X_C}{69.5+X_C^2} - \frac{6}{100} = 0$.

So, this is the Y . So, now you just your what you call this one you multiply numerator and denominator by $8 \text{ minus } j 6$. Here also numerator and denominator you multiply by $8.34 \text{ plus } j X C$. Then you simplify you will get this is the real part and this is the imaginary part. And at resonance this imaginary part will be 0 right. Therefore, if this of this part is 0, then $X C \text{ upon } 69.5 \text{ plus } X C \text{ square minus } 6 \text{ upon } 100$ is equal to 0. If we solve it, right you will get two values of $X C$ one is (Refer Time: 19:05) so $X C$ is equal to 8.35 ohm that is equal to $1 \text{ upon } \omega_0 C$ right.

(Refer Slide Time: 19:11)

The image shows the continuation of the derivation. It starts with the equation $\frac{X_C}{69.5+X_C^2} - \frac{6}{100} = 0$. This is followed by the solution for X_C : $\therefore X_C = 8.35 \Omega = \frac{1}{\omega_0 C}$. Then, the capacitance C is calculated: $\therefore C = \frac{1}{5000 \times 8.35} = 24 \mu\text{F}$. Below this, there is a section titled "Ex-6" with a circuit diagram showing a resistor R and the text "Determine R".

So, if you solve, now that your what you call the ω_0 is given 5000 radian per second it is given. Suppose C is equal to you will get 24 microfarad right. This is the answer.

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EX-6

Determine R_L & R_C which cause the circuit to be resonant at all frequencies.

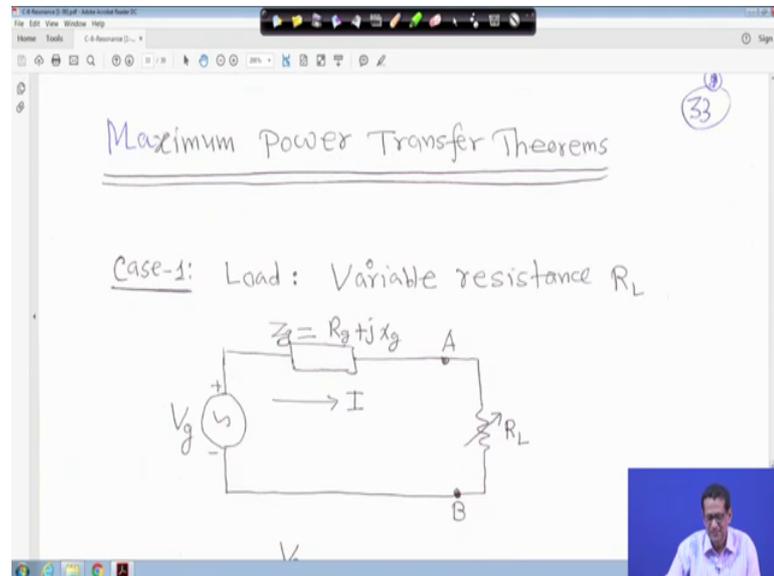
Now, next one is determine your determine R_L and R_C for this circuit R_L and R_C which causes the circuit to be resonance at all frequencies right. All frequency means that here we have derived that your what we call $1/\sqrt{LC}$ into multiplied by some factor. Now, if I recall, now I will not really hope I write correctly. If I recall correctly correct that it is \sqrt{LC} , say ω is equal to, then the factor that your $R_L^2 - L/C$ divided by $R_C^2 - L/C$ something like this.

If R_L^2 is equal to R_C^2 right is equal to L/C , so it actually resonance at all the frequency, because this square root comes it will become actually 0 by 0 undefined. So, it would circuit with resonance will happen at in all frequencies right (Refer Time: 20:17) you have to find out what is the R_L and R_C this one this condition. So, answer is not given here I given intentionally I did not write the answer. So, please do it whenever you do it, let us know the answer I will tell you the correct answer (Refer Time: 20:28) right.

So, with this with this your resonance part is over. So, some typical examples we have seen after that very simple thing it is that is the maximum power transfer theorem for DC circuit we have seen. So, for AC circuit also very simple it is we will see the

maximum power transfer theorem. Concept is from that D C we have already started. So, A C we will see little bit.

(Refer Slide Time: 20:54)



So, this is the maximum power transfer theorem for A C circuit. Now, there are 2 3 cases 3 cases; so, case 1 load right. The variable resistance is R_L suppose this is my voltage source V_0 is given for a circuit, plus minus polarity is marked current flowing through this I . And this is Z_g is equal to say R_g plus $j x g$ impedance is given, and this R_L is variable right. In the case of D C circuit, because in D C supply. And this was also your what you call this is R Thevenin this is one V Thevenin in the case of your D C circuit.

So, here also suppose this is given and then what will be your value of R_L for the maximum power transfer theorem right. So, if you see the current magnitude, I will be equal to V_g approximate that angle is 0, V_g angle 0 right. If you and it should not be in confusion in here right this will be V_g angle 0 degree that we have take in the magnitude. So, current is I is equal to V_g upon this is the series impedance together, so R_g plus R_L plus $j x g$ right. So, this is my current magnitude.

(Refer Slide Time: 21:59)

$$I = \frac{V_g}{(R_g + R_L) + jX_g}$$
$$\therefore |I| = \frac{V_g}{\sqrt{(R_g + R_L)^2 + X_g^2}}$$
$$P = |I|^2 R_L = \frac{V_g^2 R_L}{(R_g + R_L)^2 + X_g^2}$$
$$\frac{dP}{dR_L} = 0$$

Now, now your what you call, therefore your this one is just hold on. This is the given phasor this is actually then we put angle 0 degree, because V_g I told you angle 0 degree, this is a phasor because we have put j , so it is it is phasor quantity not magnitude. Now when you take the magnitude, you will take the absolute right. It is V_g upon root over R_g plus R_L square plus X_g square right. So, this is the magnitude, therefore power actually across R_L always across at R_L in magnitude I square into R_L . So, this can be V_g square into R_L by R_g plus R_L square plus X_g square right.

(Refer Slide Time: 22:40)

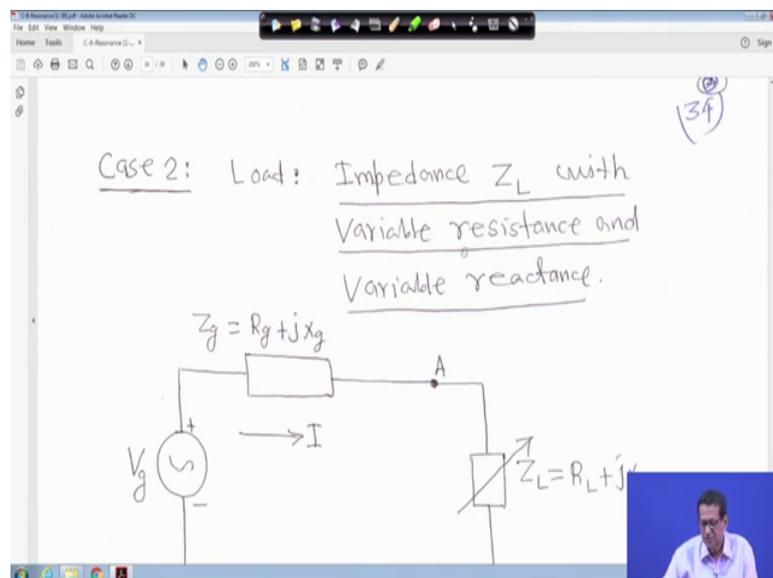
$$P = |I|^2 R_L = \frac{V_g^2 R_L}{(R_g + R_L)^2 + X_g^2}$$
$$\frac{dP}{dR_L} = 0$$
$$\therefore R_L^2 = R_g^2 + X_g^2$$
$$\therefore R_L = \sqrt{R_g^2 + X_g^2} = |Z_g|$$

If $X_g = 0$, $\therefore R_L = R_g$,

Now, for maximum power transfer theorem dP upon dR_L is equal to 0 right. If you solve if you make it 0, you will get R_L square, you will get R_g square plus X_g square that means R_L is equal to root over R_g square plus X_g square, and that is equal to magnitude of Z_g . Because, $Z_g = R_g + jX_g$, so its magnitude Z_g is equal to root over it is capital R root over R_g square plus it is it is capital, X it is also capital X capital X_g square right, so that is why R_L is equal to root over your sorry magnitude of Z_g right.

And for like your if X_g is equal to 0 like your DC maximum power transfer theorem, the naturally R_L is equal to your R_g . There we do (Refer Time: 23:28) in that case it was R_L is equal to (Refer Time: 23:31) what DC circuit (Refer Time: 23:32) similar thing. So, this is actually for that means that means for this circuit you have to keep it in mind, for this kind of circuit R_L will be your root over R_g square plus jX_g square is equal to mod g right. But, never be never be R_L is equal to R_g right it will be root over mod g root over R_g square, it will be mod g root over R_g square plus X_g square R_L is equal to right. So, this is your R_L .

(Refer Slide Time: 24:03)



So, now case 2; then in this case, that impedance Z_L with variable resistance and variable reactance. So, here also here also your what you call this is also my V_g angle 0, angle is not shown here, polarity is shown here. And this is suppose jX_g is equal to R_g plus jX_g right. It is something like your v (Refer Time: 24:21) and j (Refer time: 24:22)

say this the current I and this Z L is variable both R L and X L are variable right, so that is why that is that is that is given here, impedance Z L is variable resistance and variable reactor both are variable. So, so we have to find out the value of your what you call that your what you call the impedance right. So, now current I is equal to V g upon then you add R g plus R L plus j x g plus j x l, like your series circuit whatever you do.

(Refer Slide Time: 24:54)

$$I = \frac{V_g}{(R_g + R_L) + j(X_g + X_L)}$$

$$\therefore |I| = \frac{V_g^2}{\sqrt{(R_g + R_L)^2 + (X_g + X_L)^2}}$$

$$\therefore P = |I|^2 R_L = \frac{V_g^2 R_L}{(R_g + R_L)^2 + (X_g + X_L)^2} \quad \dots (i)$$

So, this is my this thing. So, magnitude of the current I your what you call here one, here one this thing is there. This should not be there. right. So, it is vg upon your what you call and here if you want, you can put this one this angle 0. So, magnitude of I is equal to V g upon root over R g square plus R L square plus x g plus X L square right. Now, P is equal to your I square R L is equal to V g square R L divided by R g plus R L square plus x g plus X L square this is equation 1 right. So, let me. So, this is not a square this is here well here I correct here I forgot. So, this is not there V g upon this 1. It is understandable to you.

(Refer Slide Time: 25:45)

$$V_{(R_g+R_L)^2+(X_g+X_L)^2}$$
$$\therefore P = |I|^2 R_L = \frac{V_g^2 R_L}{(R_g+R_L)^2 + (X_g+X_L)^2} \quad \dots (i)$$

If R_L in Eqn(i) is held fixed, the Value of P is maximum when $X_g = -X_L$.

So, now if R_L in equation 1 this equation is held fixed, suppose R_L we have fixed in it say R_L is held fixed. The value of P is maximum when X_g is equal to minus X_L . So, if you said X_g is equal to minus X_L that means, X_g plus X_L is equal to 0. So, this term will vanish, therefore, power is maximum if R_L is held fixed right. So, in that case the value of the P is maximum, because X_g minus X_L X_g is equal to minus X_L means X_g plus X_g plus X_L is equal to 0 I mean this term will not be there. So, in that case it will be V_g square upon R_L by R_g plus R_L square.

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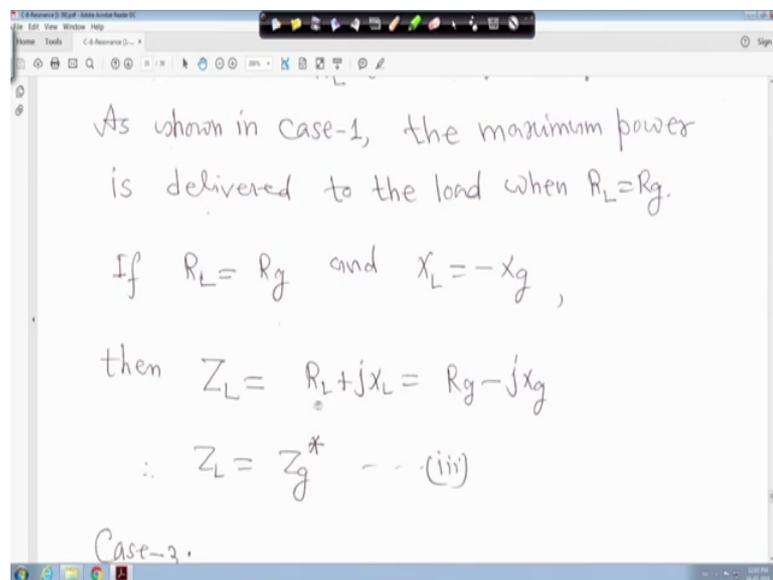
Then Eqn(i) becomes

$$P = \frac{V_g^2 R_L}{(R_g + R_L)^2} \quad \dots (i)$$

Consider now R_L to be variable,
As shown in case-1, the maximum power is delivered to the load when $R_L = R_g$.

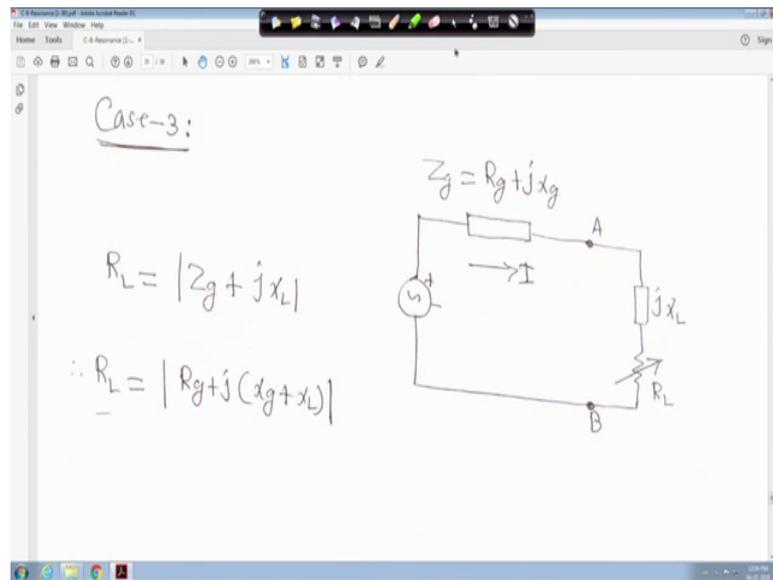
If R_L is held fixed, so that means, equation one will become your V_g^2 upon this is v_g^2 into R_L upon $R_g + R_L$ square this is equation 2 right. Now, if you as consider now R_L to be variable right (Refer Time: 26:34) in DC circuit R_L to be variable. As shown in case 1 the maximum power is delivered to the load when R_L will be is equal to R_g , there also you said for the first case X_g is equal to f_0 then R_L is equal to R_g . In that case, your what we call that X_L is equal to that means, therefore the maximum power is delivered to the load R_L is equal to R_g . If R_L is equal to R_g , and X_L is equal to minus X_g .

(Refer Slide Time: 27:01)



Then Z_L is equal to $R_L + jX_L$ here is the circuit there, Z_L is equal to $R_L + jX_L$. And here you put X_L is equal to minus X_g for maximum part of the theorem. So, here if we put that X_L is equal to your what you call minus X_g , then Z_L is equal to $R_g - jX_g$ then Z_L is equal to Z_g conjugate, because your Z_g actually is equal to your $R_g + jX_g$. Therefore, Z_g conjugate is equal to $R_g - jX_g$ right that is why for maximum power transfer theorem, when both R_L and your X_L your both are your what we call variable, then this is the condition for maximum power transfer maximum power transfer that Z_L is equal to Z_g conjugate right.

(Refer Slide Time: 27:57)



Another one is the case 3. In this case in this case your Z_L is there, where X_L is fixed, but R_L is variable. This is the case 3. So, in that case, you please do it. So, in that case you directly add this one, you will get R_g plus $j X_g$ plus X_L . So, in that case what will happen, R_L will become absolute Z_g plus $j X_L$. So, R_L will be R_g plus $j X_g$ X_L this you can do yourself. Therefore, my R_L will be is equal to maximum power transfer theorem, it will be R_g square plus X_g plus it is capital is taken does not matter this one is square. This is this is for maximum transfer straight forward we are writing like this right. This your this your this thing and this thing your right. So, it will be R_g plus $j X_g$ plus X_L right. So, these three cases is R there right.

So, in the now with this thing, we will take (Refer Time: 28:54) few simple your simple example three four example. Suppose in the circuit of figure 1 that is this is figure 1 I show you. The load Z_L consists of a pure resistance R_L . Find the value of R_L for which the source delivers maximum, it will be to this maximum power right power is using. So, maximum power to the load, determine the value of the maximum power P also right. So, let me clear it.

So, this is the circuit is given. This is $10 \angle 20^\circ$ ohm, and this is Z_L is given R_L that means, it is basically simply R_L right. And this is the source $50 \angle 0^\circ$ volt. So, we know R_L is equal to mod Z_g . So, it will be mod 10 plus $j 20$. So, root over 10 square plus 20 square. So, 22.4 ohm it will come. Therefore, I is equal to V_g upon your that is

your what we call Z_g plus R_L . So, $Z_g = 10 + j20$, and R_L we got 22.4, so it will be $1.31 \angle -31.7^\circ$ ampere right. And therefore, P is equal to $I^2 R$, so $1.31^2 \times 22.4$ is equal to 22.4, so it is 38.5 Watt. It is a very very simple problem very simple problem right.

Similarly, example 2; in this case repeat example 1 with Z_L is equal to R plus $j \times l$. R_L and X_L are both variables I mean you repeat this example when Z is equal to your R_L plus $j \times l$ added, and all data remains same, all data remains same right. So, in this case your what you can do is that your total impedance your we know that for the this one R_L and X_L both are variable. So, my Z_g was $10 + j20$ and your $j20$, therefore Z_L is equal to Z_g conjugate that will be $10 - j20$ right.

This way we have seen in our theory therefore, total impedance will be Z_g plus Z_L Z_g is $10 + j20$ and Z_L will be $10 - j20$, so $-j20$ plus $j20$ cancels it will be 20 ohm. Therefore, I will be is equal to $50 \angle 0^\circ$ by Z_T that is 20 only, so it will be $2.5 \angle 0^\circ$ ampere. And P is equal to $I^2 R$, so that is why I^2 is 25 square, and this is 10, so it will be that is R_L 10 ohm it will be 62.5 Watt.

So, only these condition repeat just keep it in mind then everything will find simple right. So, now another thing in the circuit shown in figure this 2 this is figure 2 right. The resistance R_g is variable that means, this resistance R_g is variable between 2 and 55 ohm that means R_g actually that means, if you write like this that means that means, your R_g is lying in between these two, and 55 ohm right. Then what value of R_g results in maximum power transfer across the terminal ab . This is my terminal A and this is my B . And this is my R_g variable R_L is 10 ohm this is my your X_g 5 ohm right.

So, in this case your what you call voltage is given $10 \angle 0^\circ$. In the network shown in figure 3 the load connected across terminals AB consists of a variable resistance R_L right. R_L and your what you call and a capacitive reactance X_C right. So, in that your what you call, and which is variable between 2 ohm sorry this one, just one minute this one actually your this problem sorry this problem actually I have not solved you have to find it out this is you have to find it out right. This problem actually you find it out this is not solved here right. So, this is this is an exercise for you this is solving right. So, now, next problem is example answer is not given here answer is not given here. So, this is for you actually solve it. I have not solved it here. Actually solve, but I did not put it here

you solve it. Now, example 4 in the network shown in figure 3; suppose the load connected across terminal A B consists of a variable resistance R_L and a capacitive reactance X_C I will show you which is a variable between 2 ohm, and 8 ohm.

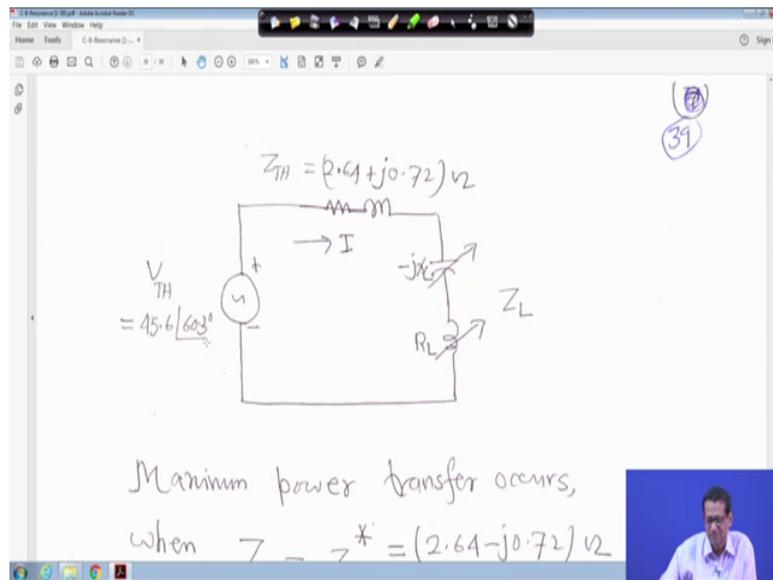
Determine the value of the R_L and X_C , which result in maximum power transfer you have to calculate the maximum power P delivered to the load. This is the problem your what we call written here right. And this is the circuit, this is voltage $50 \angle 45^\circ$. This is 3 ohm this is minus $j x c$ variable, and this is R_L . $j x c$, and R_L variable, and this is your 2 ohm $j 10$ ohm. (Refer Time: 33:38) these two are variable. This is the point A, and this is the point B, and this is the circuit. Now, question is that what is first one is to find out the v (Refer Time: 33:47) v (Refer Time: 33:48) means that we have solve for DC circuit.

So, v (Refer Time: 33:52) means first you remove this one. Suppose it is not there, first you remove it. So, as soon as you remove it then you find out what is the current I right. So, the current I am writing here current I is equal to your $50 \angle 45^\circ$ divided by this is $3 + 2 + j 10$ right. This is the current I right, because this is not there because we are reopening, because on to get the (Refer Time: 34:20) So, this is the current I . So, once you get the current, so this is open circuit I am not drawing the circuit again.

So, this is my V_{AB} this is my v (Refer Time: 34:29), because this is open this is open this is nothing is there. So, this is A, this is B. So, it is V_{AB} is equal to v (Refer Time: 34:36). So, this is my current this is my current I into this is my voltage that is my sorry this is my impedance that is my $2 + 0$ ohm whatever it comes right. So, same thing is written here $50 \angle 45^\circ$. This $3 + 5 + j 10$ so, this is $5 + j 10$ into $2 + j 10$ into $2 + j 10$. This is my v (Refer Time: 34:57) right. So let me clear it.

So, this is my (Refer Time: 35:03) we will got $45.6 \angle 60.3^\circ$ degree your Z (Refer Time: 35:07) is equal to when this one is not there when this one this point this is open (Refer Time: 35:13) mean you have to (Refer Time: 35:15) DC circuit it is started right. So, it will be three open $2 + j 2$ means parallel. So, it will be 3 into $2 + j 10$ right divided by $3 + 2 + j 10$ right. So, this is my your this is my Z (Refer Time: 35:31) right. So, if you find out Z (Refer Time: 35:36). So, this will be my your what we call Z (Refer Time: 35:39) $2.64 + j 0.72$ ohm.

(Refer Slide Time: 35:47)



Then the equivalent circuit is this V (Refer Time: 35:45) 45.6 angle 60.3 degree. And this is my Z (Refer Time: 35:49) 2.64 plus j point 7.2 . And both variable R L V also variable X is also variable. So, for maximum power if both are variable. So, for maximum power transfer you know Z_L is equal to z (Refer Time: 36:02) in this case conjugate, because this is Z (Refer Time: 36:04).

So, it is conjugate, so it will be 2.64 minus $j 7.2$ ohm, but now $x C$ is adjustable between 2 ohm and 8 ohm. So, the closest value of $x C$ is 2 ohm right, because we will get actually what you call, it is 0.72 , but $x C$ only variable between 2 and 8 ohm. So, closest value is 2 ohm only, because as it is 0.7 . So closest value is 2 ohm so, $x C$ is taken as 2 ohm right, therefore right.

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X_c is adjustable between 2 Ω and 8 Ω
Hence the closest value of X_c is 2 Ω
and
 $R_L = |Z_g - jX_c| = |2.64 + j0.72 - j2|$
 $\therefore R_L = |2.64 - j1.28| = 2.93 \Omega$
 $Z_T = Z_{TH} + Z_L = 2.64 + j0.72 + 2.93 - j2$

Therefore, R_L is equal to mod Z_g minus $j x c$ you have already done it; you forget R_L and X_L are variable. So, in this case, it will be 2.64 plus $j 0.72$ minus $j x c$ is equal to taken 2 ohm right, so that means, my R_L will become 2.93 ohm. Therefore, Z_T will become Z_{TH} (Refer Time: 36:52) plus Z_L ; Z_{TH} (Refer Time: 36:53) is this one, this 2.64 plus $j 0.72$ and (Refer Time: 36:59) Z_L will become 2.93 minus $j 2$, because some range is given, here you got something, here you got something, but closest value is 2 (Refer Time: 37:07) X_C in between 2 and 8 right.

(Refer Slide Time: 37:13)

$\therefore R_L = |2.64 - j1.28| = 2.93 \Omega$
 $Z_T = Z_{TH} + Z_L = 2.64 + j0.72 + 2.93 - j2$
 $\therefore Z_T = 5.57 - j1.28 = 5.7 \angle -13^\circ \Omega$
 $\therefore I = \frac{45.6 \angle 60^\circ}{5.7 \angle -13^\circ} = 8 \angle 73^\circ \text{ Amp.}$
 $P = (8)^2 \times 2.93 = 187.5 \text{ Watt.}$

Therefore, your what you call that the you calculate I now Z T got this value, you got this value. Then you get I this one (Refer Time: 37:21) your Z T, you will get 8 angle 73.3 degree ampere. And power is equal to your 8 square in to 2.93 that is 187.5 watt.

Thank you very much; we will be back.