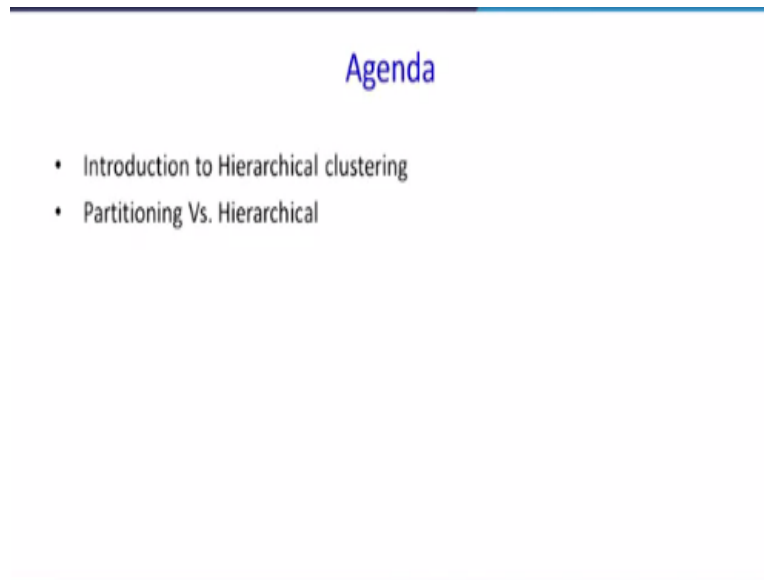


Data Analytics with Python
Prof. Ramesh Anbanandam
Department of Management Studies
Indian Institute of Technology - Roorkee

Lecture – 55
Hierarchical Method of Clustering - I

In our previous lecture, I have explained about K - means algorithm that is one type of clustering technique.

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There is another type of technique is hierarchical method of clustering, let us see what is hierarchical method of clustering in this lecture and we will compare that partitioning method versus hierarchical clustering methods in this lecture. So, the agenda for this lecture is introduction to hierarchical clustering, then comparison of partitioning versus hierarchical clustering methods.

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Introduction

- A hierarchical method creates a hierarchical decomposition of the given set of data objects
- A hierarchical clustering method works by grouping data objects into a tree of clusters
- A hierarchical method can be classified as being either agglomerative or divisive, based on how the hierarchical decomposition is formed
- The agglomerative approach, also called the bottom-up approach, starts with each object forming a separate group

A hierarchical method creates a hierarchical decomposition of the given set of data objects, a hierarchical clustering method works by grouping data objects into tree of clusters. Here the tree of clusters, I will explain what is this tree of clusters in next slides. A hierarchical method can be classified as being either agglomerative or divisive, based on how the hierarchical decomposition is formed.

There are 2 way we can say in hierarchical method, one is agglomerative, the second one is divisive, the agglomerative approach also called bottom up approach, start with each object forming a separate group.

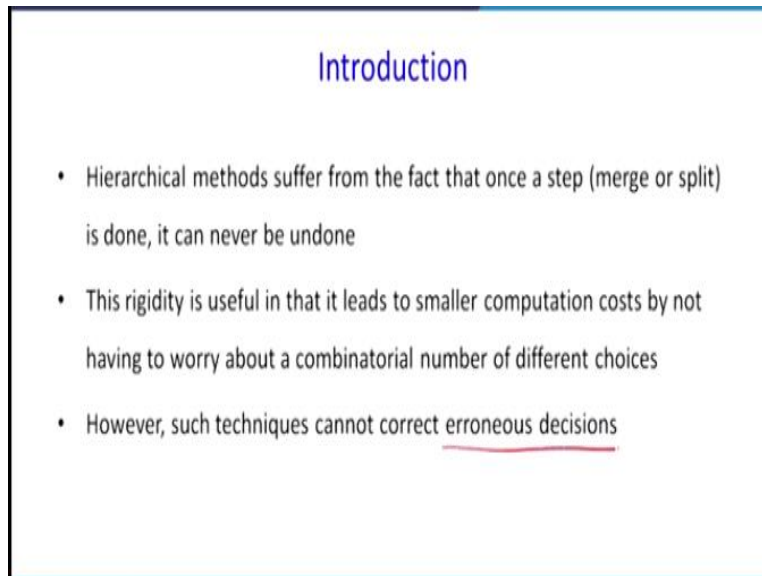
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Introduction

- It successively merges the objects or groups that are close to one another, until all of the groups are merged into one (the topmost level of the hierarchy), or until a termination condition holds
 - The divisive approach, also called the top-down approach, starts with all of the objects in the same cluster
 - In each successive iteration, a cluster is split up into smaller clusters, until eventually each object is in one cluster, or until a termination condition holds
-

It successively merges the objects or groups that are close to one another, until all of the groups are merged into the top most level of the hierarchy or until a termination condition holds, on the other hand, the another classification in the hierarchical method is in divisive approach also called top down approach starts with of the objects in the same cluster. In each successive iteration, a cluster is split up into smaller clusters, until eventually each object is in one cluster.

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The slide is titled "Introduction" in blue text. It contains three bullet points:

- Hierarchical methods suffer from the fact that once a step (merge or split) is done, it can never be undone
- This rigidity is useful in that it leads to smaller computation costs by not having to worry about a combinatorial number of different choices
- However, such techniques cannot correct erroneous decisions

Or until a termination condition hold, hierarchical methods suffer from the fact that once a step is done, it can never be undone, so the problem with the hierarchical cluster is once a step is done, you cannot go back and correct the mistake. This rigidity is useful in that it leads to smaller computation cost by not having to worry about combinatorial number of different choices, however, such techniques cannot correct erroneous decisions that is only drawback of this hierarchical methods.

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Agglomerative and Divisive Hierarchical Clustering

<p>Agglomerative </p> <ul style="list-style-type: none"> • This bottom-up strategy starts by placing each object in its own cluster and then merges these atomic clusters into larger and larger clusters, until all of the objects are in a single cluster or until certain termination conditions are satisfied • Most hierarchical clustering methods belong to this category 	<p>Divisive Hierarchical </p> <ul style="list-style-type: none"> • This top-down strategy does the reverse of agglomerative hierarchical clustering by starting with all objects in one cluster • It subdivides the cluster into smaller and smaller pieces, until each object forms a cluster on its own or until it satisfies certain termination conditions, such as a desired number of clusters is obtained or the diameter of each cluster is within a certain threshold
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Let us compare agglomerative method versus divisive method, both are hierarchical method; let us see how this it is differ from each other. The agglomerative method this is bottom up strategy starts by placing each object in its own cluster and then merges these atomic clusters into larger and larger clusters until all of the objects are in a single cluster or until certain termination condition is satisfied.

Most hierarchical clustering methods belong to this category, on the other hand, the divisive method is a top down strategy does the reverse of agglomerative hierarchical clustering by starting with all object in one cluster. So, in divisive methods what we are doing, so you start from a bigger cluster, then you make smaller one, like it is a cutting a big cake into small pieces. On the other hand, the agglomerative is each object is separate clusters.

Then from that you can form all possible types of clusters that is kind of a tree, it is up to you to decide where you need to have the termination condition. In the divisive method, the divisive method sub divides the cluster into smaller and smaller pieces until each object forms a cluster on its own or until it satisfy certain termination condition such as a desired number of cluster is obtained or the diameter of each cluster is within the certain threshold.

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Agglomerative versus divisive hierarchical clustering

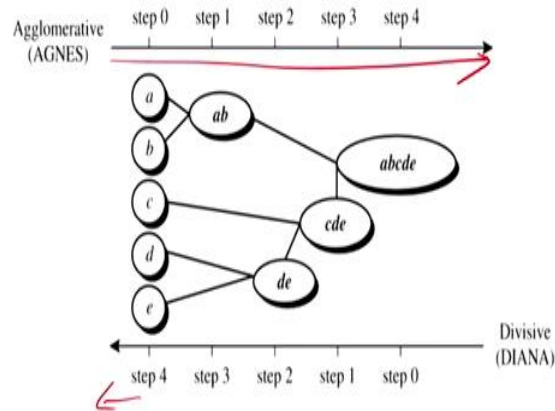


Figure: 1 Agglomerative and divisive hierarchical clustering on data objects {a,b,c,d,e}

This picture explains the difference between agglomerative and divisive method, you see that the arrow for agglomerative method is going on this side, it says that there are a, b, c, d, there are 5 objects, we start with each objects are in a separate cluster, then this a and b in step 0, all are clusters; 1, 2, 3, 4, 5 cluster is there, each cluster having only 1 unit. In step 1, see a and b are clubbed that is ab.

In step 2, d and e are clubbed, in step 3 this c, d, e are clubbed, in step 4 all these a, b, c, d is clubbed, so this is going in from left to right that is agglomerative method whereas in the divisive method, you start from; you see that look at this arrow it is going this side, start from the a, b, c, d that is a big by considering all the elements. A step 0; look at the step 0, only one cluster, in step 1, the c, d, e is 1, in step 2 de is another cluster. In step 3, from a, b, c, d again the ab has come out, in step 4 all individual elements are separate clusters that is a basic difference between agglomerative versus divisive hierarchical clustering.

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Interpretation

- Figure: 1 shows the application of AGNES (AGglomerative NESTing), an agglomerative hierarchical clustering method, and DIANA (Dlvisive ANALysis), a divisive hierarchical clustering method, to a data set of five objects, {a,b,c,d,e}
- Initially, AGNES places each object into a cluster of its own
- The clusters are then merged step-by-step according to some criterion
- Let's say for example, clusters C_1 and C_2 may be merged if an object in C_1 and an object in C_2 form the minimum Euclidean distance between any two objects from different clusters

What is the interpretation of the previous slides? Figure 1 shows that application of (()) (06:29) AGNES; agglomerative nesting, an agglomerative hierarchical clustering methods and DIANA divisive analysis, a divisive hierarchical clustering method to a data set of 5 objects; a, b, c, d, e. Initially, agglomerative method places each object into a cluster of its own, there is only one item. The clusters at then merged step by step according to some criterion, let us say for example, cluster C_1 and C_2 may be merged if an object C_1 and the object C_2 from the minimum Euclidean between any 2 objects from different clusters.

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Interpretation

- This is a single-linkage approach in that each cluster is represented by all of the objects in the cluster, and the similarity between two clusters is measured by the similarity of the closest pair of data points belonging to different clusters
- The cluster merging process repeats until all of the objects are eventually merged to form one cluster

This is a single linkage approach, in that each cluster is represented by all of the objects in the cluster and the similarity between 2 cluster is measured by the similarity of the closest pair of the

data points belonging to different clusters. The cluster merging process repeats until all of the objects are eventually merged into form 1 cluster. So, what is happening here it is start from the step 0, it goes up to step 4, you see in step 0, there are 1, 2, 3, 4, 5 clusters in step 0.

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Interpretation

- In DIANA, all of the objects are used to form one initial cluster
- The cluster is split according to some principle, such as the maximum Euclidean distance between the closest neighboring objects in the cluster
- The cluster splitting process repeats until, eventually, each new cluster contains only a single object
- In either agglomerative or divisive hierarchical clustering, the user can specify the desired number of clusters as a termination condition

But in step 1, all are merged into only 1 cluster that is a, b, c, d, e. In DIANA that is in the divisive method, all of the objects are used to form 1 initial cluster, this cluster split according to some principle such as maximum Euclidean distance between the closest neighbouring objects in the cluster. The cluster splitting process repeats until eventually each new cluster contains only 1 object, only a single object.

In either agglomerative or divisive hierarchical clustering, the user can specify the desired number of clusters as a termination condition. So, here the explanation of divisive method is start from here, in step 0 only 1 cluster is there. In step 4, there are 5 clusters is there, that is a difference.

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Dendrogram

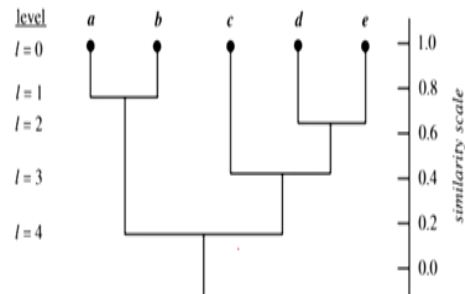


Figure 2: Dendrogram representation for hierarchical clustering of data objects{a,b,c,d,e}

In hierarchical clustering, another important terminology which you have to understand is dendrogram. What is a dendrogram? It is a kind of a tree kind of structure and it says there are different levels, level 0, 1, 2, 3, 4 on left hand side and right hand side there is a similarity scale. At level 0, there are 1, 2, 3, 4, 5 clusters a, b, c, d, e all are forming its own cluster. In level 1, ab is forming 1 cluster.

In level 2, the position of c is compared, in the position of c we are finding the distance between c and between these cluster a and b and cluster d and e. If it is closer to d and e, then c, d, e form an another cluster that is a level 3. Level 4, it is only 1 cluster, all are 5 elements are present in there, so this kind of picture is called dendrogram.

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Dendrogram

- A tree structure called a dendrogram is commonly used to represent the process of hierarchical clustering
- It shows how objects are grouped together step by step
- Figure: 2 shows a dendrogram for the five objects presented in Figure:1 , where $l=0$ shows the five objects as singleton clusters at level 0
- At $l=1$, objects a and b are grouped together to form the first cluster, and they stay together at all subsequent levels

Dendrogram, a tree structure called a dendrogram is commonly used to represent the process of hierarchical clustering; it shows how objects are grouped together step by step. Figure 2 shows a dendrogram for the 5 objects presented in the figure 1, where l equal to 0, at level 0 shows the 5 objects are singleton clusters, there is only 1 element in the clusters at level 0. At level 1, object a and b are grouped together to form the first cluster and they stay together at all subsequent levels, this hierarchical structure can be understood with the help of this dendrogram.

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Dendrogram

- We can also use a vertical axis to show the similarity scale between clusters
- For example, when the similarity of two groups of objects, $\{a,b\}$ and $\{c,d,e\}$, is roughly 0.16, they are merged together to form a single cluster

We can also use a vertical axis to show the similarity scale between the clusters actually, it is given on the right hand side of the picture. For example, when the similarity of 2 groups of object a and b and c, d, e is roughly 0.16, so they merged together to form a single cluster.

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Measures for distance between clusters

- Four widely used measures for distance between clusters are as follows, where $|p-p'|$ is the distance between two objects or points, p and p' , m_i is the mean for cluster, C_i and n_i is the number of objects in C_i
- Minimum distance: $d_{\min}(C_i, C_j) = \min_{p \in C_i, p' \in C_j} |p-p'|$
- Maximum distance: $d_{\max}(C_i, C_j) = \max_{p \in C_i, p' \in C_j} |p-p'|$
- Mean distance: $d_{\text{mean}}(C_i, C_j) = |m_i - m_j|$
- Average distance: $d_{\text{avg}}(C_i, C_j) = \frac{1}{n_i n_j} \sum_{p \in C_i} \sum_{p' \in C_j} |p-p'|$

Now, let us go to another important idea of measures of distance between clusters, there are 4 widely used measures for distance between clusters are as follows, where modulus of $p - p$ dash is the distance between 2 objects or points that is a p and p dash, where m_i is the mean of the cluster, C_i and n_i is the number of objects in C_i . The first measure is minimum distance, the minimum distance between cluster C_i and C_j equal to, so minimum of modulus of $p - p$ dash.

The maximum distance is d_{\max} between cluster i and j equal to maximum of modulus of $p - p$ dash, the mean distance; there is a another measure is d_{mean} is the modulus of mean of the 2 clusters. The average distance is 1 divided by $n_i - n_j$, here n represents number of object in cluster 1, then sigma of $p - p$ dash modulus.

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Measures for distance between clusters

- When an algorithm uses the minimum distance, $d_{\min}(C_i, C_j)$, to measure the distance between clusters, it is sometimes called a nearest-neighbor clustering algorithm
- Moreover, if the clustering process is terminated when the distance between nearest clusters exceeds an arbitrary threshold, it is called a single-linkage algorithm
- If we view the data points as nodes of a graph, with edges forming a path between the nodes in a cluster, then the merging of two clusters, C_i and C_j , corresponds to adding an edge between the nearest pair of nodes in C_i and C_j

When an algorithm uses the minimum distance that is a d_{\min} between C_i and C_j , that is a distance between C_i and C_j . To measure the distance between clusters, it is sometime called nearest neighbour clustering algorithm, I will show you in picture in coming slides. Moreover, if the clustering process is terminated, when the distance between the nearest clusters exceeds the arbitrary threshold, it is called single linkage algorithm.

If we view the data points as nodes of graph with edges forming a path between the nodes in a cluster, then the merging of 2 clusters; C_i and C_j corresponds to adding an edge between the nearest pair of nodes C_i and C_j .

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Measures for distance between clusters

- Because edges linking clusters always go between distinct clusters, the resulting graph will generate a tree
- Thus, an agglomerative hierarchical clustering algorithm that uses the minimum distance measure is also called a minimal spanning tree algorithm
- When an algorithm uses the maximum distance, $d_{\max}(C_i, C_j)$, to measure the distance between clusters, it is sometimes called a farthest-neighbor clustering algorithm
- If the clustering process is terminated when the maximum distance between nearest clusters exceeds an arbitrary threshold, it is called a complete-linkage algorithm

Because edges linking clusters always go between distinct clusters, the resulting graph will generate a tree, thus an agglomerative hierarchical clustering algorithm that uses the minimum distance measure is also called minimal spanning tree algorithm, even in your subject operation research also, there is a topic network problems in the (()) (13:27) minimal spanning tree algorithm.

When an algorithm uses the maximum distance between cluster i and j , to measure the distance between clusters, it is sometime called farthest neighbour clustering algorithm. If the clustering process is terminated, when the maximum distance between nearest cluster exceeds an arbitrary threshold, it is called complete linkage algorithm.

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Measures for distance between clusters

- By viewing data points as nodes of a graph, with edges linking nodes, we can think of each cluster as a complete sub graph, that is, with edges connecting all of the nodes in the clusters
- The distance between two clusters is determined by the most distant nodes in the two clusters
- Farthest-neighbor algorithms tend to minimize the increase in diameter of the clusters at each iteration as little as possible
- If the true clusters are rather compact and approximately equal in size, the method will produce high-quality clusters
- Otherwise, the clusters produced can be meaningless

By viewing data points as nodes of graph with edges linking nodes, we can think of each cluster as a complete sub graph that is with edges connecting all of the nodes in the cluster. The distance between 2 cluster is determined by the most distant nodes in the 2 clusters, farthest neighbour algorithm tend to minimise the increase in diameter of the clusters at each iteration as little as possible. If the true clusters are rather compact and approximately equal in size, the method will produce high quality clusters, otherwise the clusters produced can be meaningless.

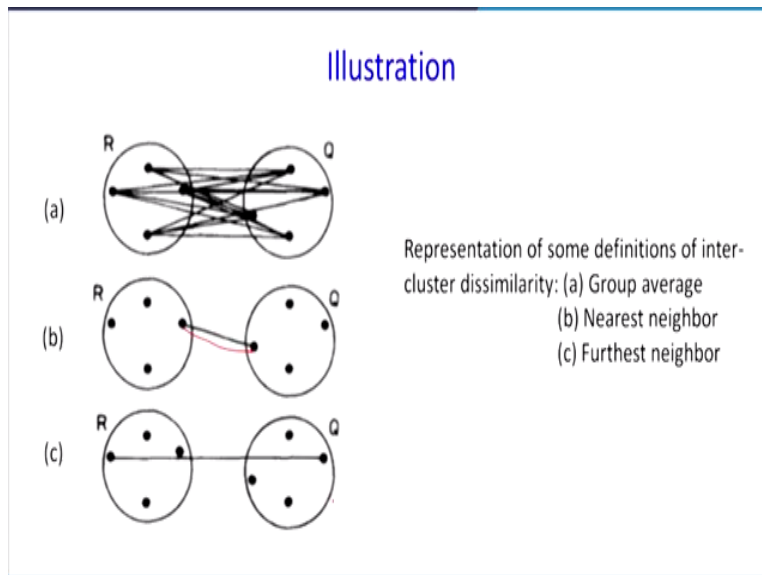
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Choice of measurement

- The above minimum and maximum measures represent two extremes in measuring the distance between clusters
- They tend to be overly sensitive to outliers or noisy data
- The use of mean or average distance is a compromise between the minimum and maximum distances and overcomes the outlier sensitivity problem
- Whereas the mean distance is the simplest to compute, the average distance is advantageous in that it can handle categorical as well as numeric data

Let us go for choice of measurement; the above minimum and maximum measure represents 2 extremes in measuring the distance between clusters, they tend to be overly sensitive to outliers or noisy data. The use of mean or average distance is a compromise between minimum and maximum distances and overcome the outlier sensitivity problems, whereas the mean distance is the simplest to compute, the average distance is advantageous in that it can handle categorical as well as numeric data.

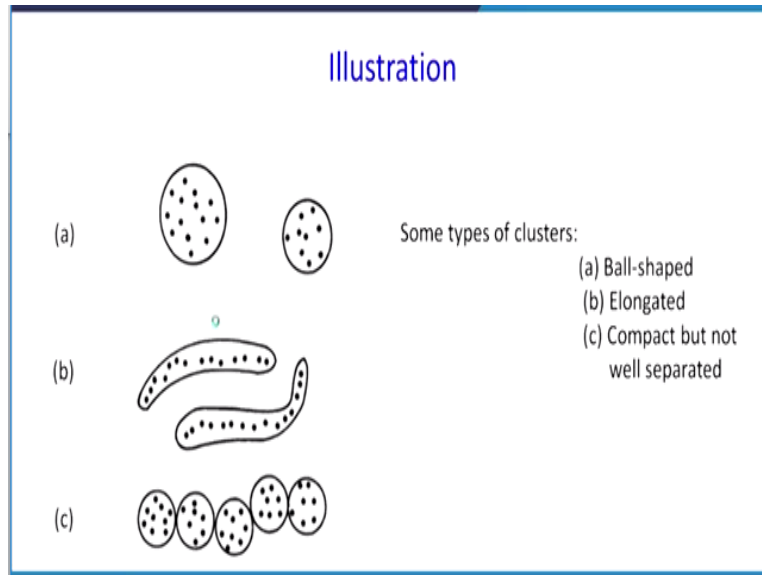
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This picture shows the distance measures, see the first one represents group average, so you see that all the points are connected with all other points in that cluster. This R is one cluster; Q is one cluster you see that we have finding the beverage that is a group average. This is

representation of some definition of inter cluster dissimilarity. The second one is the nearest neighbour. See, this is a nearest neighbour, the third one is the farthest neighbour that I have explained in my previous slides, this is a different type of distance measures.

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So, this picture shows some type of clusters, see the cluster here is the ball shaped one, the second one is elongated one the last one is compact but not well separated. So, what will happen; if we follow the group average, your; the final cluster may be this shape, what is that; the ball shaped one. If we follow this distance measures that is a nearest neighbour, the final cluster may look like this one that is elongated.

You see that any time, it can form with this point any time we can go to that other cluster, in case if you follow the farthest neighbour distance measures, your final cluster may be in this format that is a compact but not well separated, that is why choosing the correct distance is more important, based on the your distance measures, your shape of final cluster also will vary.

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Difficulties with hierarchical clustering

- The hierarchical clustering method, though simple, often encounters difficulties regarding the selection of merge or split points
- Such a decision is critical because once a group of objects is merged or split, the process at the next step will operate on the newly generated clusters
- It will neither undo what was done previously nor perform object swapping between clusters

The difficulties with the hierarchical clustering; the hierarchical clustering method, though simple often encounters difficulties regarding the selection of merge or split points, such a decision is critical because once a group of object is merged or split, the process at the next step will operate on the newly generated clusters. As I told you, this also one of the drawback, once the cluster is formed, you cannot, any mistake has happened that cannot be rectified if you follow hierarchical clustering methods. See it will neither undo what was done previously nor perform objects swapping between clusters; these are the some of the disadvantages of hierarchical clustering.

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Difficulties with hierarchical clustering

- Thus merge or split decisions, if not well chosen at some step, may lead to low-quality clusters
- Moreover, the method does not scale well, because each decision to merge or split requires the examination and evaluation of a good number of objects or cluster
- For improving the clustering quality of hierarchical methods is to integrate hierarchical clustering with other clustering techniques, resulting in multiple-phase clustering

Thus, merge or split decisions if not well chosen at some step may lead to low quality clusters, moreover, the method does not scale well because each decision to merge or split requires the examination and the evaluation of good number of objects or clusters. For improving the cluster quality of hierarchical method is to integrate hierarchical clustering with other clustering techniques resulting in multiple phase clustering. So, what we can do; if you want to improve the quality of hierarchical clustering, it can be clubbed with other clustering algorithms, so that you can improve the quality of our clustering.

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Partitioning Vs. Hierarchical

Method	General Characteristics
Partitioning methods	<ul style="list-style-type: none">- Find mutually exclusive clusters of spherical shape- Distance-based- May use mean or medoid (etc.) to represent cluster center- Effective for small- to medium-size data sets
Hierarchical methods	<ul style="list-style-type: none">- Clustering is a hierarchical decomposition (i.e., multiple levels)- Cannot correct erroneous merges or splits- May incorporate other techniques like microclustering or consider object "linkages"

Now, let us compare the partitioning clustering algorithm versus hierarchical clustering algorithm, first we will see what is this partitioning methods, what are the general characteristics that is a K means algorithm is a partitioning method. Find mutually exclusive cluster of spherical shape, this partitioning method is a distance based, may use mean or medoid to represent cluster center, effective for small to medium sized dataset.

Hierarchical methods; clustering is a hierarchical decomposition at multiple levels, cannot correct erroneous merges or splits, may incorporate other techniques like micro clustering, consumer object linkages.

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K-means versus Hierarchical clustering

Let us compare K means versus hierarchical clustering.

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K means versus hierarchical clustering

K- means clustering

- Non-hierarchical methods-(k-means), using a pre-specified number of clusters
- This method assigns records to each cluster to find the mutually exclusive cluster of spherical shape based on distance
- In this case, one can use mean or median as a cluster centre to represent each cluster

Hierarchical clustering

- Hierarchical methods can be either agglomerative or divisive
- Agglomerative methods begin with 'n' clusters and sequentially merge similar clusters until a single cluster is obtained

K means clustering; it is a non-hierarchical method because there will be K means using a pre specified number of clusters. So, when we doing K means clustering in advance we know, how many cluster we are going to have. This method assigns records to each cluster to find the mutually exclusive cluster of spherical shape based on distance. In K mean clustering one can use mean or median as a cluster centre to represent each cluster.

For hierarchical clustering, this method can be either agglomerative or divisive. Agglomerative method begins with n clusters and sequentially merge similar clusters until a single cluster is obtained.

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K means versus hierarchical clustering	
K- means clustering	Hierarchical clustering
<ul style="list-style-type: none">• This method is generally less computationally intensive and are therefore preferred with very large datasets	<ul style="list-style-type: none">• Divisive methods work in the opposite direction, starting with one cluster that includes all records• Hierarchical methods are especially useful when the goal is to arrange the clusters into a natural hierarchy

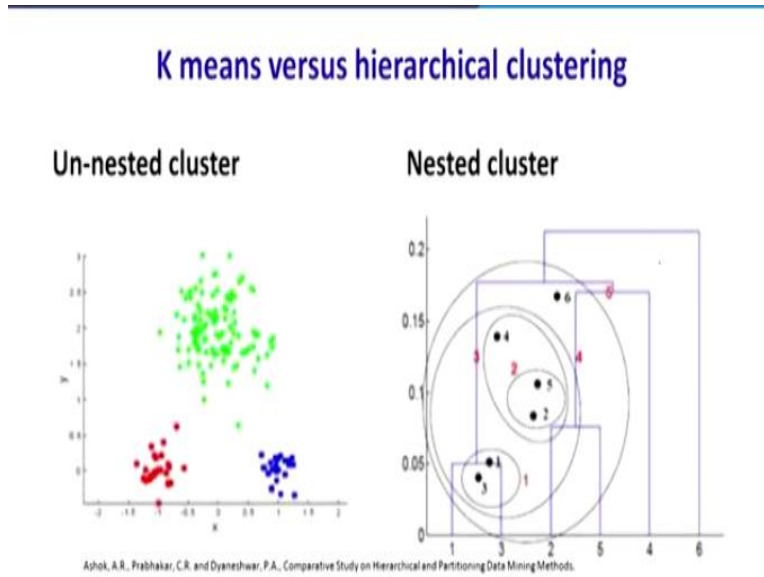
K means clustering methods is generally less computationally intensive and are therefore preferred with very large data set. In hierarchical clustering, divisive methods work in the opposite direction starting with one cluster that includes all the records. Hierarchical methods are especially useful when the goal is to arrange the cluster into a natural hierarchy.

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K means versus hierarchical clustering	
K- means clustering	Hierarchical clustering
<ul style="list-style-type: none">• A partitioning (K- means) clustering a simply a division of the set of data objects into non-overlapping subsets (clusters) such that each data object is in exactly one subset)	<ul style="list-style-type: none">• A hierarchical clustering is a set of nested clusters that are organized as a tree

A partitioning that means a K means clustering simply a division of the set of data objects into non overlapping subsets clusters such that each data object is in exactly one subset; a hierarchical clustering is a set of nested clusters that are organised as a tree.

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When you look at this picture, the picture shows in the left hand side is un-nested clusters, we can say it is a K means clusters. In the right hand side, the name is called nested cluster, this is nothing but your agglomerative or hierarchical clustering.

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K means versus hierarchical clustering

- Hierarchical clustering does not assume a particular value of 'k', as needed by k-means clustering
- The generated tree may correspond to a meaningful taxonomy
- Only a distance or "proximity" matrix is needed to compute the hierarchical clustering

	a	b	c	d	e	f
a	0	184	222	177	216	231
b	184	0	45	123	128	200
c	222	45	0	129	121	203
d	177	123	129	0	46	83
e	216	128	121	46	0	83
f	231	200	203	83	83	0

Proximity matrix

Hierarchical clustering does not assume a particular value of K as needed by K means clustering, the generated tree may correspond to a meaningful taxonomy, only a distance or proximity

matrix is needed to compute the hierarchical clustering. This is an example of proximity matrix, see the between a and a, the distance is 0, proximity 0, between b and a, the distance is 184.

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K means versus hierarchical clustering

K Means clustering

- In K Means clustering, since one start with random choice of clusters, the results produced by running the algorithm multiple times might differ
- K Means is found to work well when the shape of the clusters is hyper spherical (like circle in 2D, sphere in 3D)

Hierarchical clustering

- Results are reproducible in Hierarchical clustering
- Hierarchical clustering don't work as good as, k means when the shape of the clusters is hyper spherical

In K means clustering, since one start with random choice of clusters, the result produced by running the algorithm multiple times might differ. K means is found to work well, when the shape of the cluster hyper spherical like circle in 2 dimension, sphere in 3 dimension. In hierarchical clustering, results are reproducible, hierarchical clustering do not work as good as K means, when the shape of the cluster is hyper spherical.

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K means versus hierarchical clustering

K Means clustering

- K Means clustering requires prior knowledge of K i.e. no. of clusters one want to divide your data into

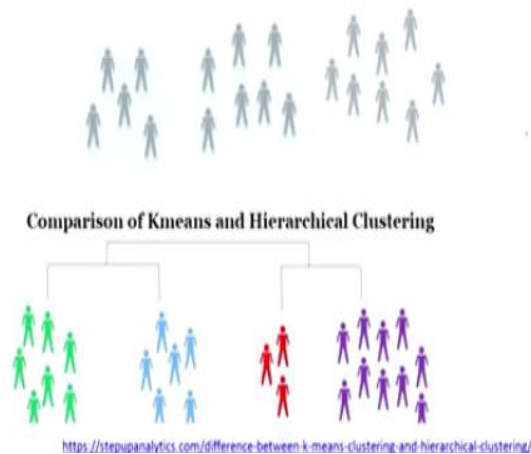
Hierarchical clustering

- In hierarchical clustering one can stop at any number of clusters, one find appropriate by interpreting the dendrogram
-

So, the K means clustering suitable for hyper spherical clustering, K means clustering requires prior knowledge of K that is number of clusters one want to divide your data into. In hierarchical clustering, one can stop at any number of clusters, one find appropriate by integrating the dendrogram.

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K means versus hierarchical clustering



There are 2 pictures, the top one is example of K means clustering where K equal to 3, the bottom one is hierarchical clustering, you see that there is a hierarchy is there, so this is an example of.

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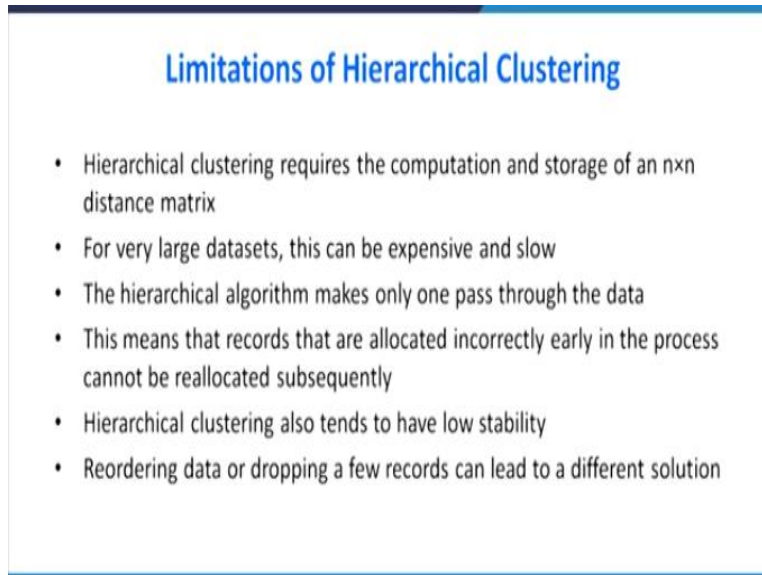
Hierarchical clustering

Advantages

- Ease of handling of any forms of similarity or distance
- Consequently, applicable to any attributes types

Advantage of hierarchical clustering; ease of handling of any form of similarity or distance, consequently applicable to any attribute types, here attribute is the variable types, it may be interval, it may be ratio, it may be binary or categorical.

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Limitations of Hierarchical Clustering

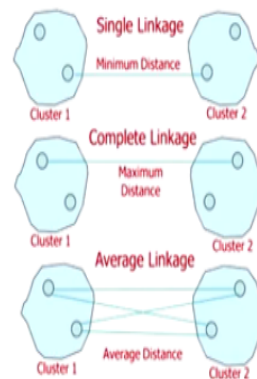
- Hierarchical clustering requires the computation and storage of an $n \times n$ distance matrix
- For very large datasets, this can be expensive and slow
- The hierarchical algorithm makes only one pass through the data
- This means that records that are allocated incorrectly early in the process cannot be reallocated subsequently
- Hierarchical clustering also tends to have low stability
- Reordering data or dropping a few records can lead to a different solution

Some of the limitations of hierarchical clustering; hierarchical clustering requires the computation and storage of n cross n distance matrix, here n is number of objects. For very large dataset this can be expensive and slow, the hierarchical algorithm makes only one pass through the data, this means that the records that are allocated incorrectly early in the process cannot be reallocated subsequently. Hierarchical clustering also tends to have low stability, reordering data or dropping a few records can lead to different solution.

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Limitations of Hierarchical Clustering

- With respect to the choice of distance between clusters, single and complete linkage are robust to changes in the distance metric (e.g., Euclidean, statistical distance) as long as the relative ordering is kept.
- In contrast, average linkage is more influenced by the choice of distance metric, and might lead to completely different clusters when the metric is changed
- Hierarchical clustering is sensitive to outlier



Limitation of hierarchical clustering; with respect to the choice of distance between clusters, single and complete linkages are robust to changes in the distance metric as long as the relative order is kept. So, what is the example of single linkage when you look at this, there is a cluster 1, cluster 2, so the minimum distance is called single linkage and the distance between the farthest points that is called complete linkage.

So, if you use these distance measure, then the cluster what you got is very robust, in contrast average linkage is more influenced by choice of distance metrics and might lead to completely different clusters when the metric is changed, hierarchical clustering is sensitive to outlier. If any extreme dataset is there that may provide different kind of clusters.

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Average-linkage clustering

- Compromise between Single and Complete Link
- Strengths
 - Less susceptible to noise and outliers
- Limitations
 - Biased towards globular clusters



Then, when we will go for average linkage clustering, what is an example of average linkage clustering? This one, you see that, all the distance are connected then we found average. It is a compromise between single and complete link. The strength of average linkage clustering is less susceptible to noise and outliers, the limitations are biased towards globular clusters. So, when you use average linkage clustering, many times, the cluster may be like a spherical shape.

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K- means clustering

Advantages

- The center of mass can be found efficiently by finding the mean value of each co-ordinate
- This leads to an efficient algorithm to compute the new centroids with a single scan of the data

Disadvantages

- K-means has problems when clusters are of differing sizes, densities, non-globular shapes and when the data contains outliers

Now, let us see the advantage of K means clustering, previously we have seen advantage of hierarchical clustering, the advantage of K means clustering is the centre of mass can be found efficiently by finding the mean value of each coordinate, this leads to an efficient algorithm to compute the new centroids with a single scan of data. The disadvantages are K means has

problem when the cluster of different sizes, densities, non- globular shapes and when the data contains outliers.

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Similarity

- Two most popular methods: hierarchical agglomerative clustering and k-means clustering
- In both cases, we need to define two types of distances: distance between two records and distance between two cluster
- In both cases, there is a variety of metrics that can be used

What is a similarity between hierarchical clustering and K means clustering; 2 most popular method is hierarchical agglomerative clustering and K means clustering, in both cases we need to define 2 types of distance, distance between 2 records and distance between 2 cluster, in both cases, there is a variety of metrics that can be used. In this lecture, I have explained introduction to hierarchical clustering.

Then, I have compared the difference between K means clustering techniques and hierarchical clustering techniques and also I have explained the advantages and disadvantages. In the next lecture, we are going to take one numerical example, with the help of numerical example; I am going to explain how to do a hierarchical clustering, thank you very much.